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# Recent Advances in Coded Aperture Correlation Holography

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Swinburne University of Technology, Australia



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# Where are we located?







# Research Group



Prof. Vijay Anand  
Group leader



Dr. Amudhavel J  
(Research fellow)



Dr. Vipin Tiwari  
(Postdoc fellow)



Dr. Viktor Palm  
(Specialist)



Dr. Praveen PA  
(Postdoc fellow)



Prof. Saulius J  
Group leader



Prof. Vijay Anand  
Adj Assoc Professor



Dr. Soon Hock Ng  
STEM fellow



Dr. Tomas Katkus  
Engineer



Mr. Tauno Kahro  
(Specialist)



Mr. Shiva G  
(Doctoral student)



Ms. Francis GA  
(Doctoral student)



Ms. Agnes PIX  
(Doctoral student)



Prof. Joseph R  
(Visiting Prof)



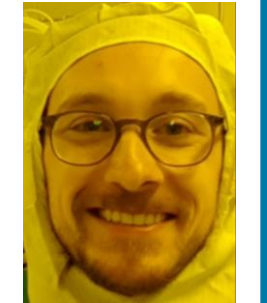
Mr. Daniel Smith  
(Jt PhD student)



Mr. Molong Han  
(Doctoral student)



Mr. Jovan M  
(Doctoral student)



Dr. Stefan L  
Defence project



Ms. Narmada J  
(Doctoral student)



Mr. Oskar T  
(Bachelor student)



Mr. Aravind Simon  
(Research manager)



Ms. Tiia Lillemaa  
(Project manager)



Prof. Kaido Reivelt  
(Coordinator)



Dr. Mani R R  
(UNC Chapel)



Dr. Angika B  
(Wake Forest)



Dr. Roy Kelner  
(TUD)



Dr. Yuval K  
(Spectralics)



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# Outline

Incoherent digital holography

Coded aperture imaging technology

Coded aperture correlation holography

Interferenceless coded aperture correlation holography

Reconstruction methods

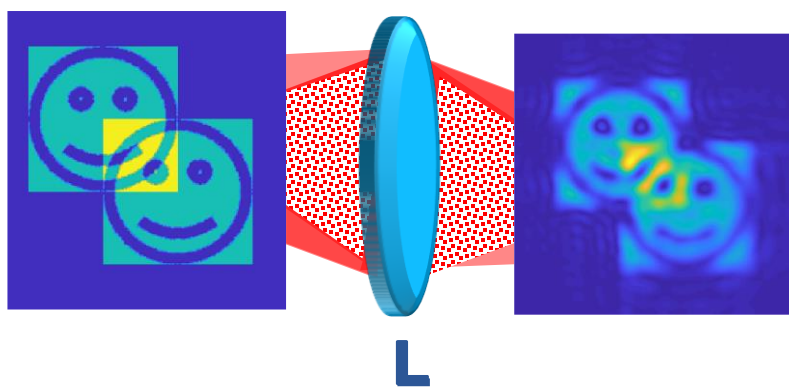
Aperture engineering

New capabilities and applications

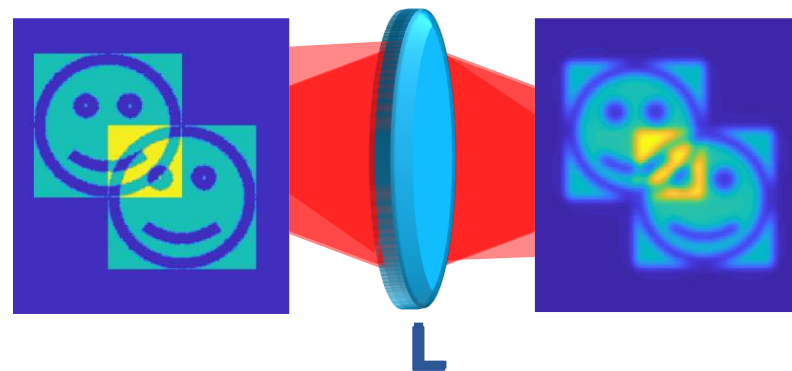


# Coherent vs Incoherent imaging

Coherent Imaging	Spatially incoherent Imaging
Needs a coherent light source such as laser	Low cost LEDs or natural light
Suffers from speckle noise	No speckle noise
Edge ringing effects	No edge ringing effects
Narrow bandwidth of MTF	Twice the bandwidth of MTF of coherent light



**A coherent imaging system is linear in complex amplitude.**



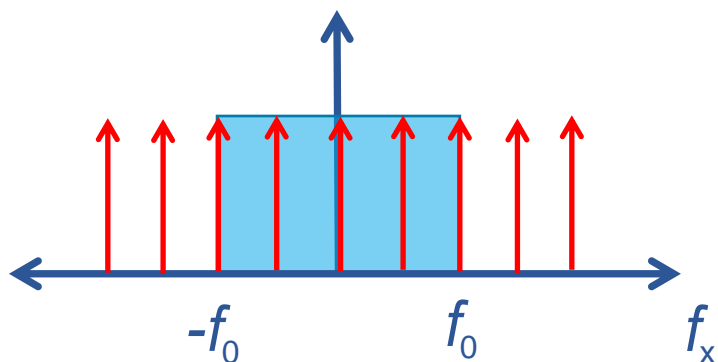
**An incoherent imaging system is linear in intensity.**

# Coherent vs Incoherent imaging

## Coherent systems

$$I_i = |h \otimes U_o|^2$$

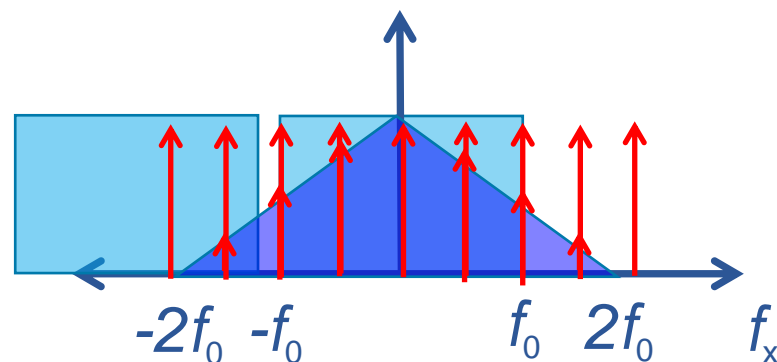
$$\mathfrak{F}\{I_i\} = [HG_o \otimes HG_o]$$



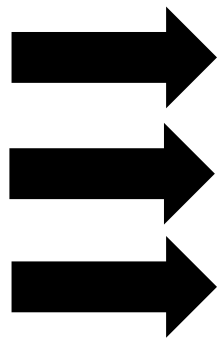
## Incoherent systems

$$I_i = |h|^2 \otimes I_o = |h|^2 \otimes |U_o|^2$$

$$\mathfrak{F}\{I_i\} = [H \otimes H][G_o \otimes G_o]$$



Coherent



Object



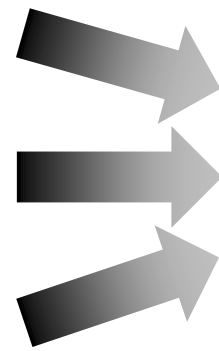
$f_0$

0

$-f_0$



Incoherent



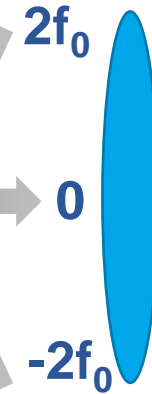
Object



$2f_0$

0

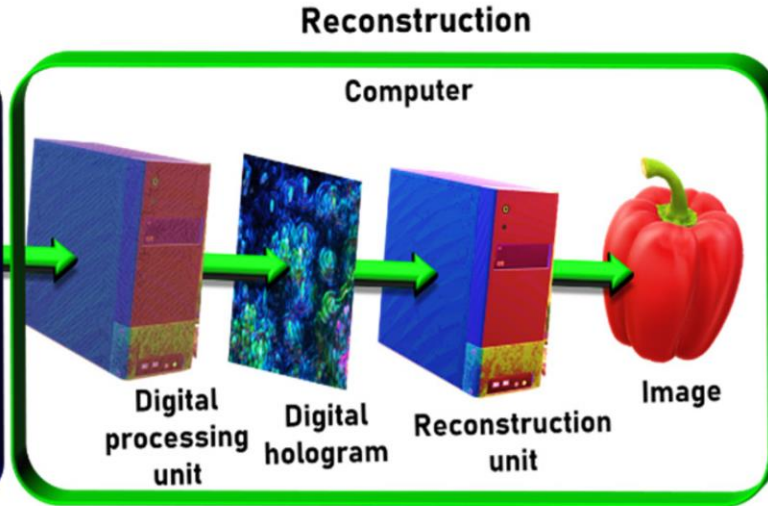
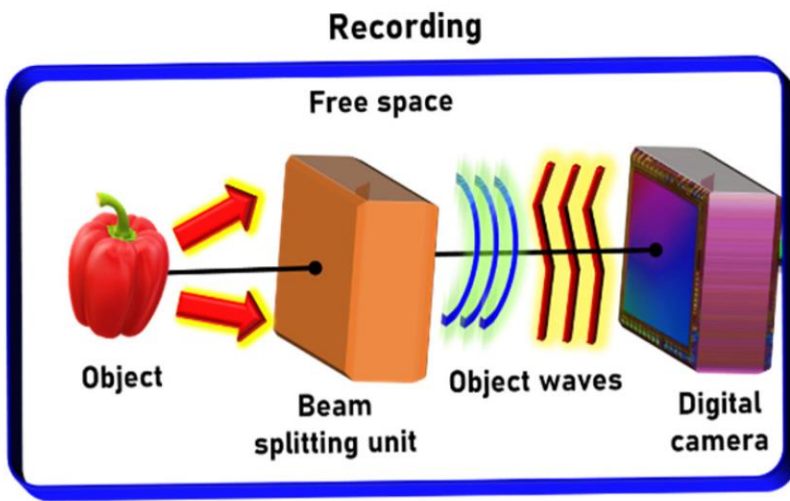
$-2f_0$



CIPHR

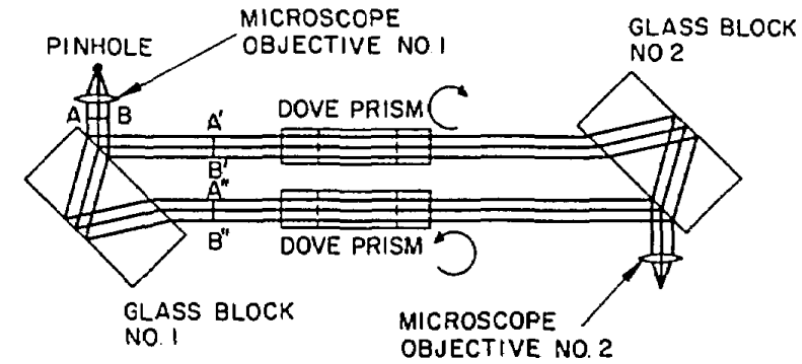


# Principle of Incoherent holography



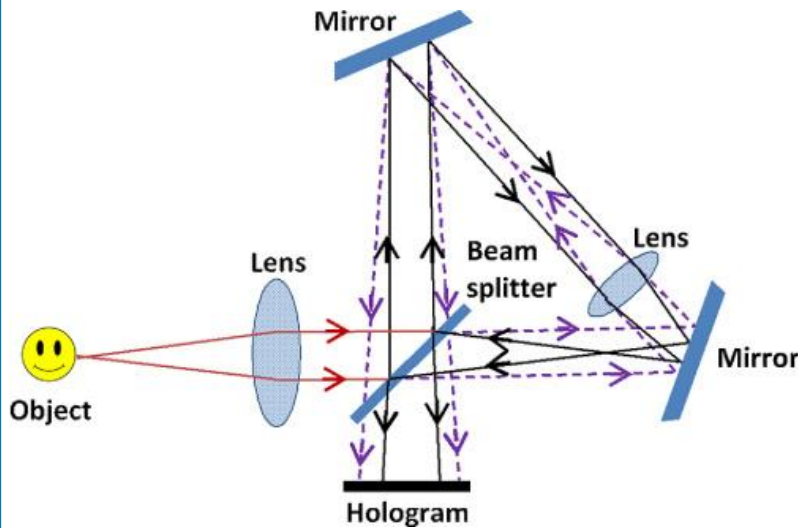
Rosen, et. al. *J. Imaging*, 7, 197 (2021)

## Rotational shearing interferometer



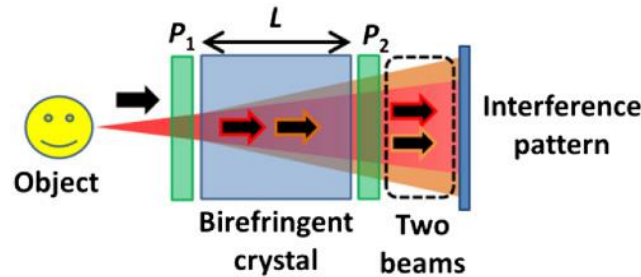
M. V. R. K. Murty and E. C. Hagerott, *Appl. Opt.* 5, 615 (1966)

## Triangle interferometer



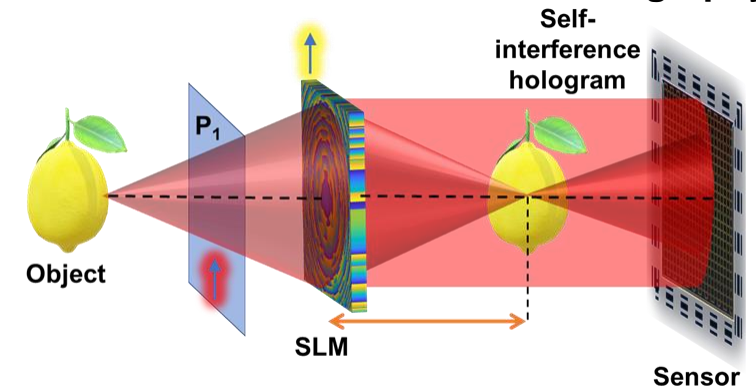
Rosen, et. al. *Adv. Opt. Photon.* 11, 1 (2019)

## Conoscopic holography



G. Y. Sirat, *J. Opt. Soc. Am. A* 9, 70 (1992).

## Fresnel incoherent correlation holography

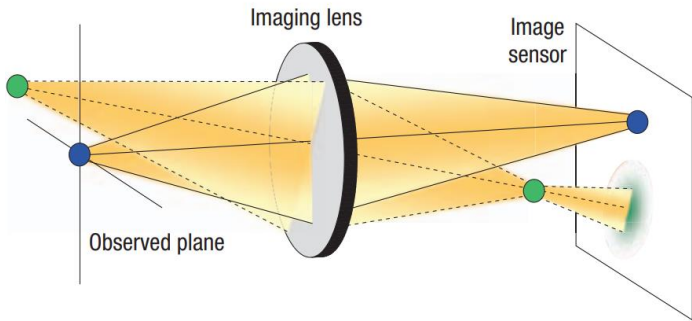


J. Rosen and G. Brooker, *Opt. Lett.* 32, 912 (2007).  
J. Rosen and G. Brooker, *Nat. Photonics* 2, 190 (2008).

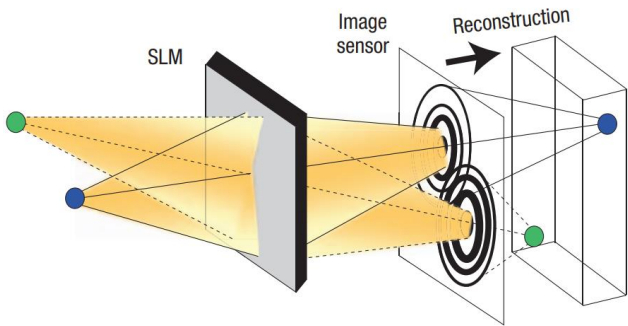


# Fresnel incoherent correlation holography

Incoherent digital holography

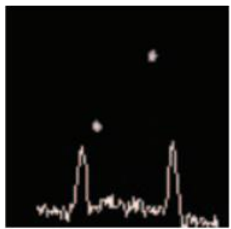


Conventional imaging

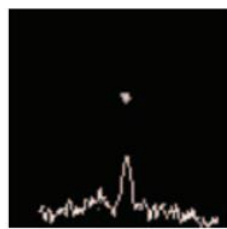


FINCH

Reconstruction results

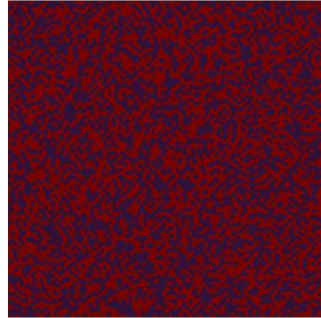


38  $\mu\text{m}$

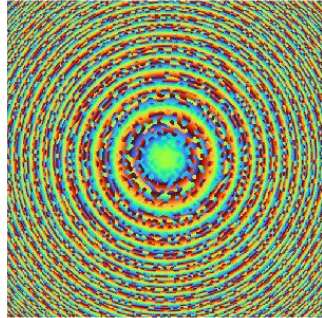


84  $\mu\text{m}$

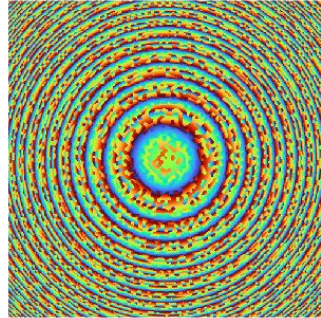
Binary random phase mask



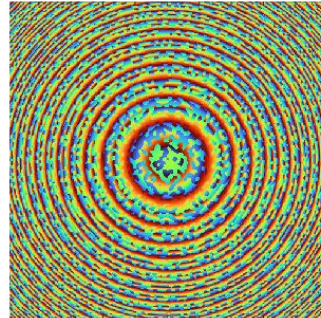
Phase mask 1  
Theta = 0 degrees



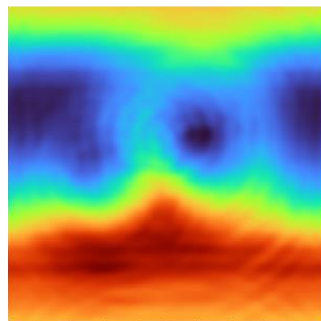
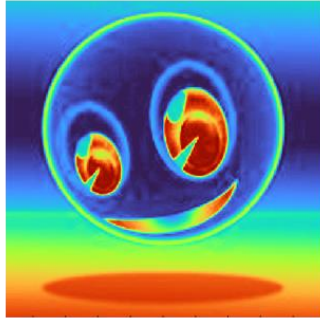
Phase mask 2  
Theta = 120 degrees



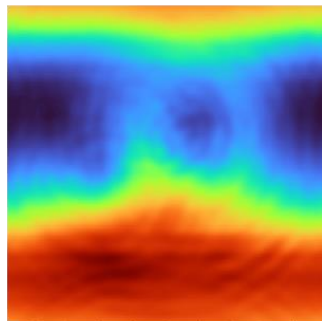
Phase mask 3  
Theta = 240 degrees



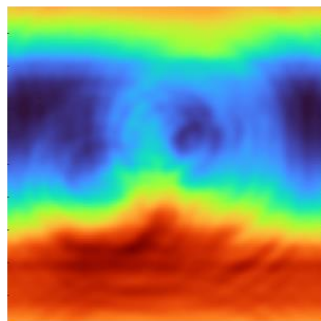
Test object



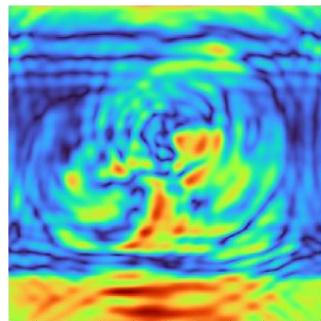
Object hologram 1  
Theta = 0 degrees



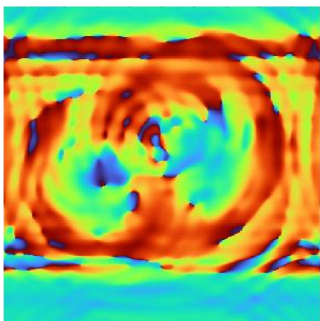
Object hologram 2  
Theta = 120 degrees



Object hologram 3  
Theta = 240 degrees

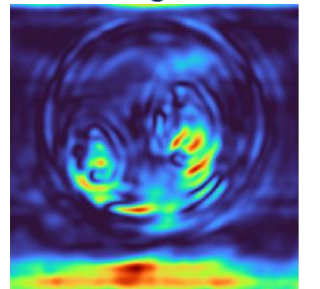


Amplitude of complex hologram



Phase of complex hologram

Rosen J, Brooker G. *Nature Photonics*. 2008;2(3):190-5.



Reconstruction result

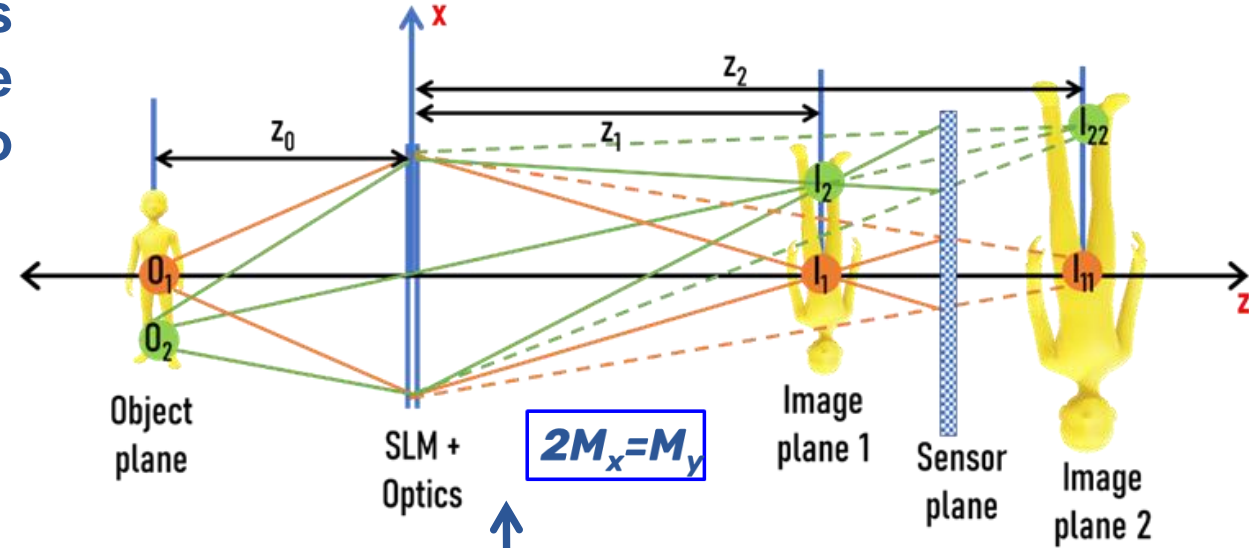
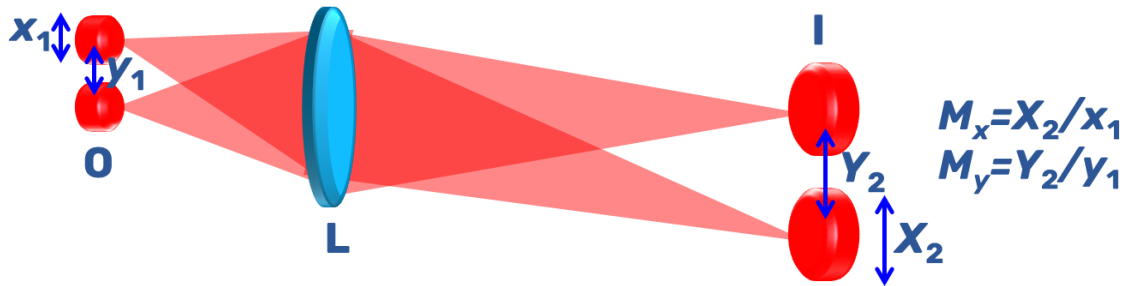




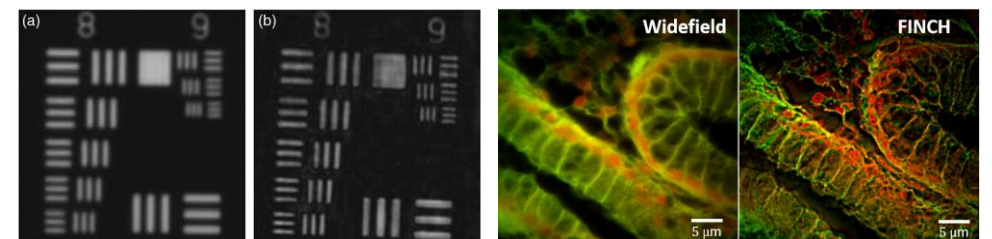
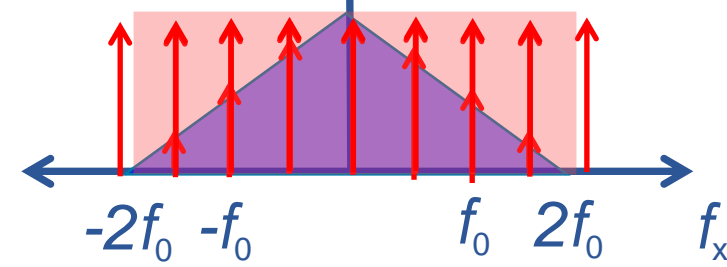
# Lagrange invariant condition and super resolution

Incoherent digital holography

Lagrange Invariant condition also called as Smith–Helmholtz formula states that the magnification of spacing between two points is same as magnification of the point.

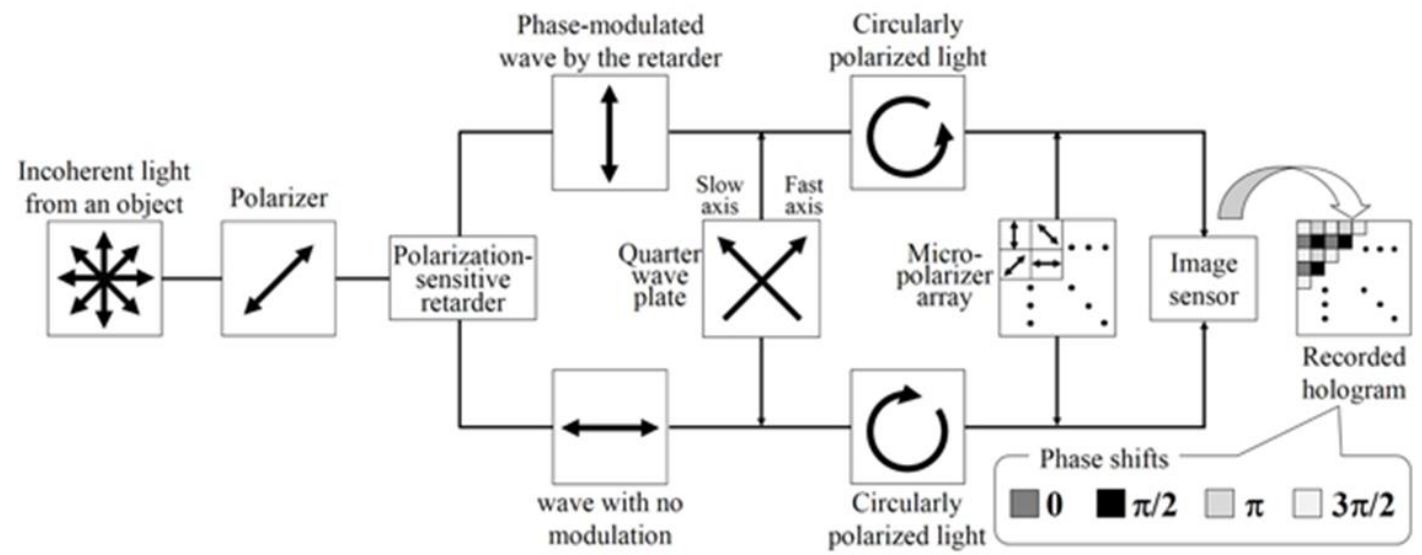
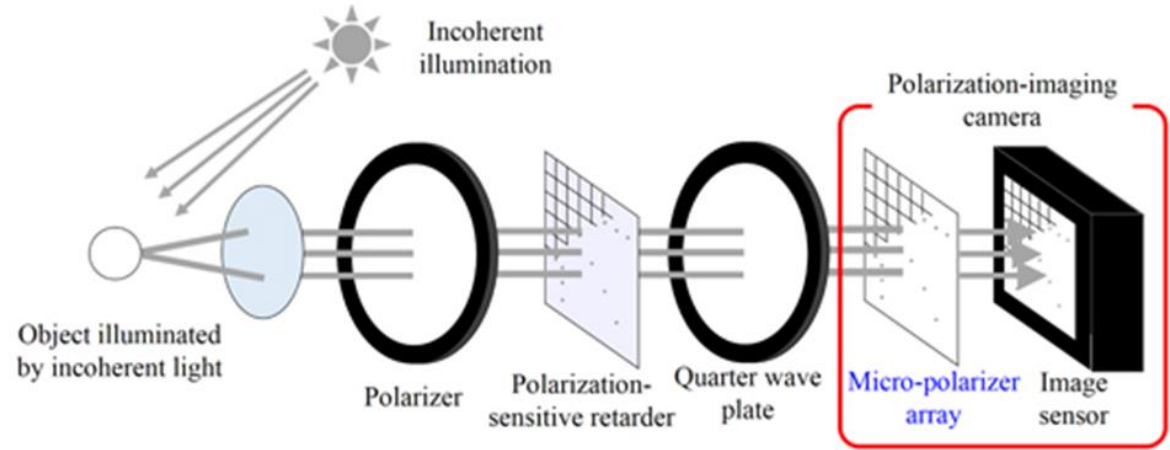
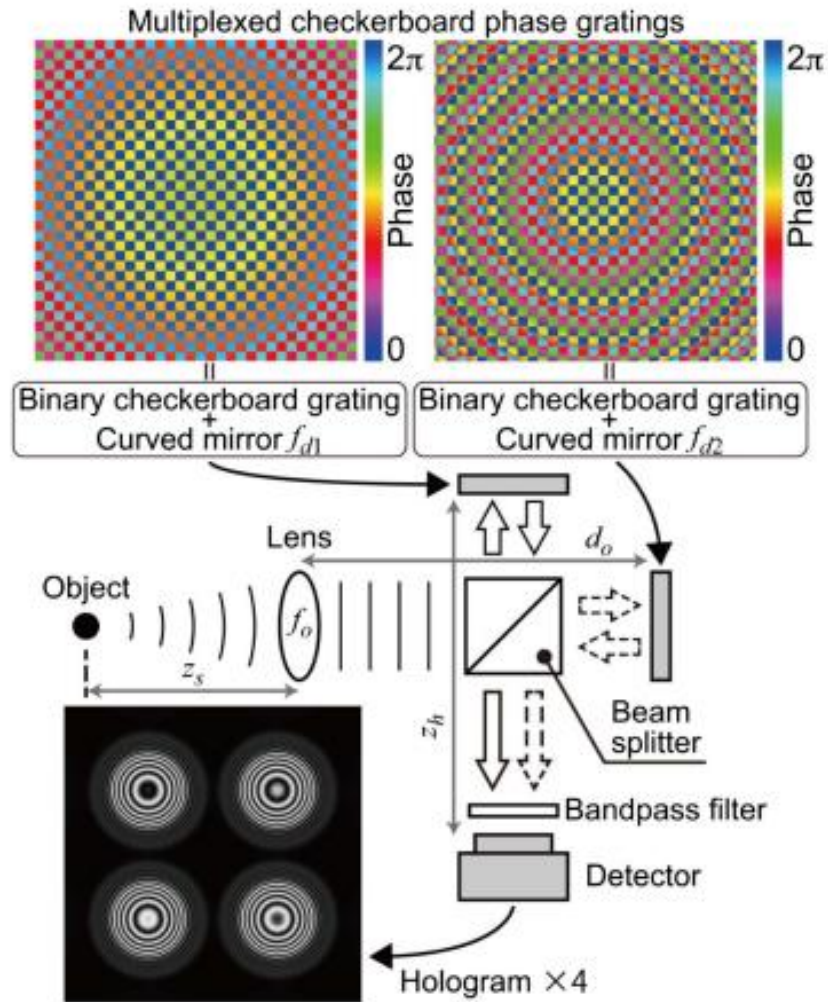


- $M_x = M_y$  Lagrange Invariant condition satisfied.
- $M_x \neq M_y$  Lagrange Invariant condition not satisfied.
- $M_x < M_y$  Lagrange Invariant condition not satisfied and super resolution.



# Evolution of FINCH – Time resolution

Incoherent digital holography



Nobukawa, et. al. *Opt. Lett.* 43, 1698-1701 (2018)

Tahara et. al. *Opt. Lett.* 2011;36:3254.





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Incoherent digital holography

Coded aperture imaging technology

Coded aperture correlation holography

Interferenceless coded aperture correlation holography

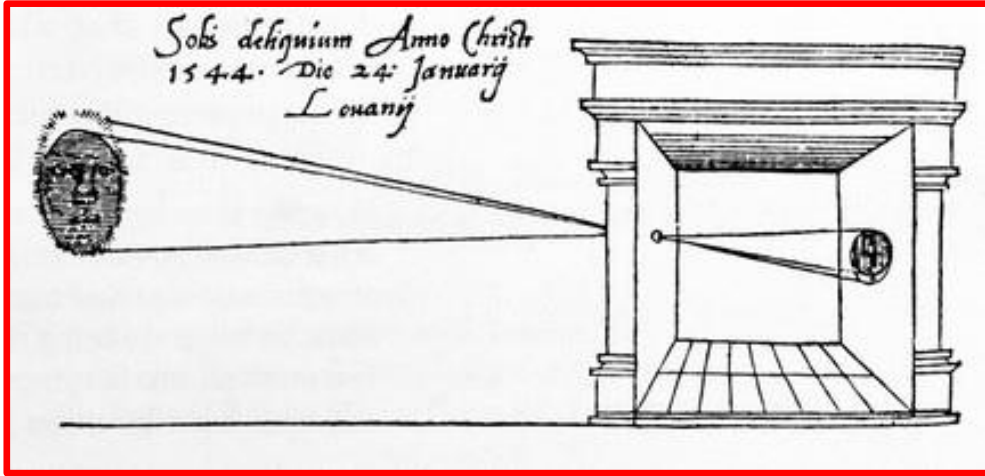
Reconstruction methods

Aperture engineering

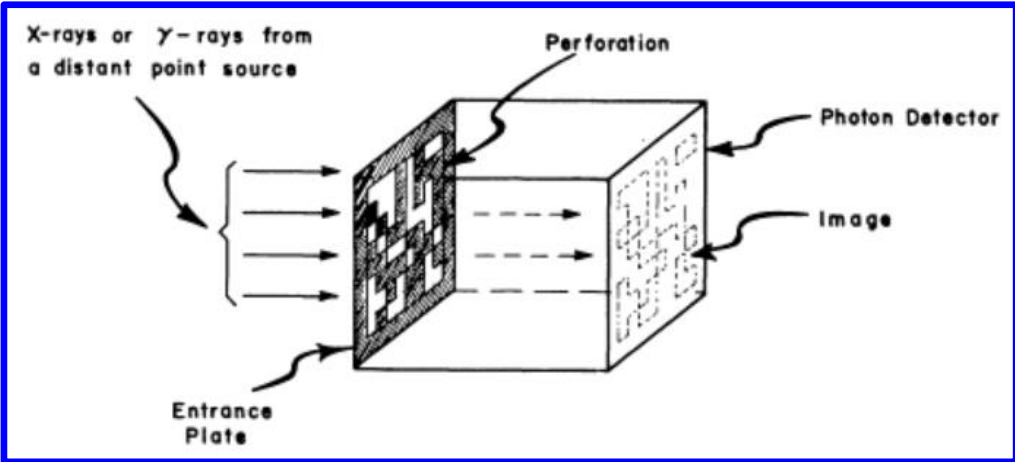
New capabilities and applications

# History of coded aperture imaging

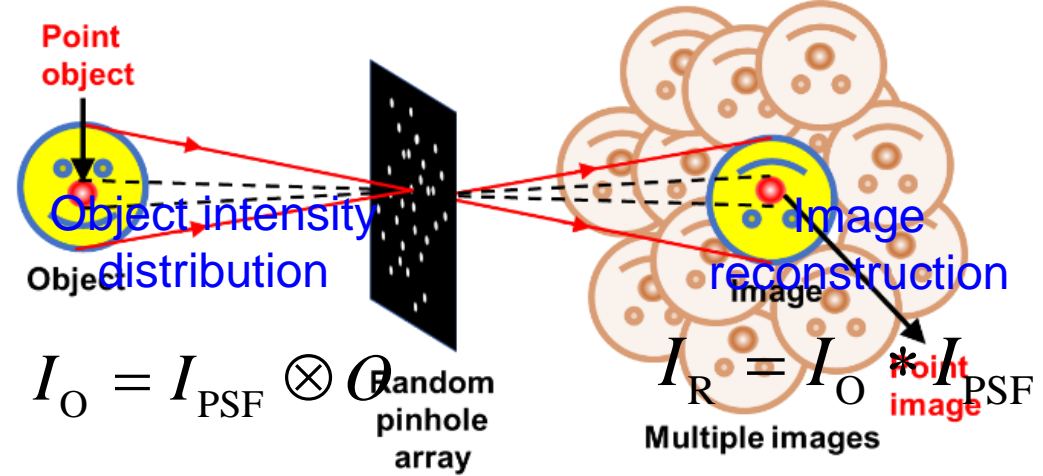
Coded aperture imaging technology



Gemma Frisius' 1545 book *De Radio Astronomica et Geometrica*

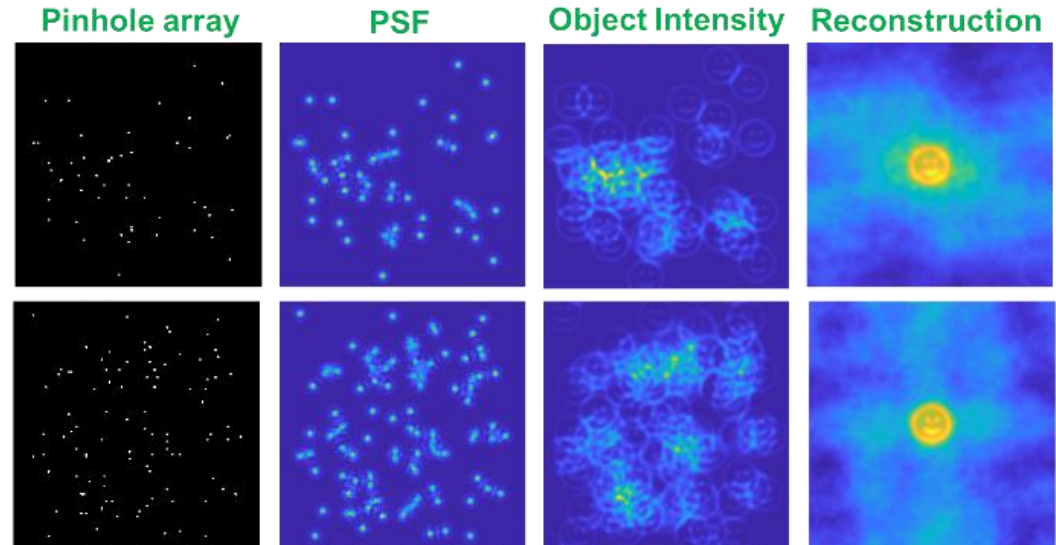


Dicke, *Astrophysical Journal*, vol. 153, p.L101 (1968)



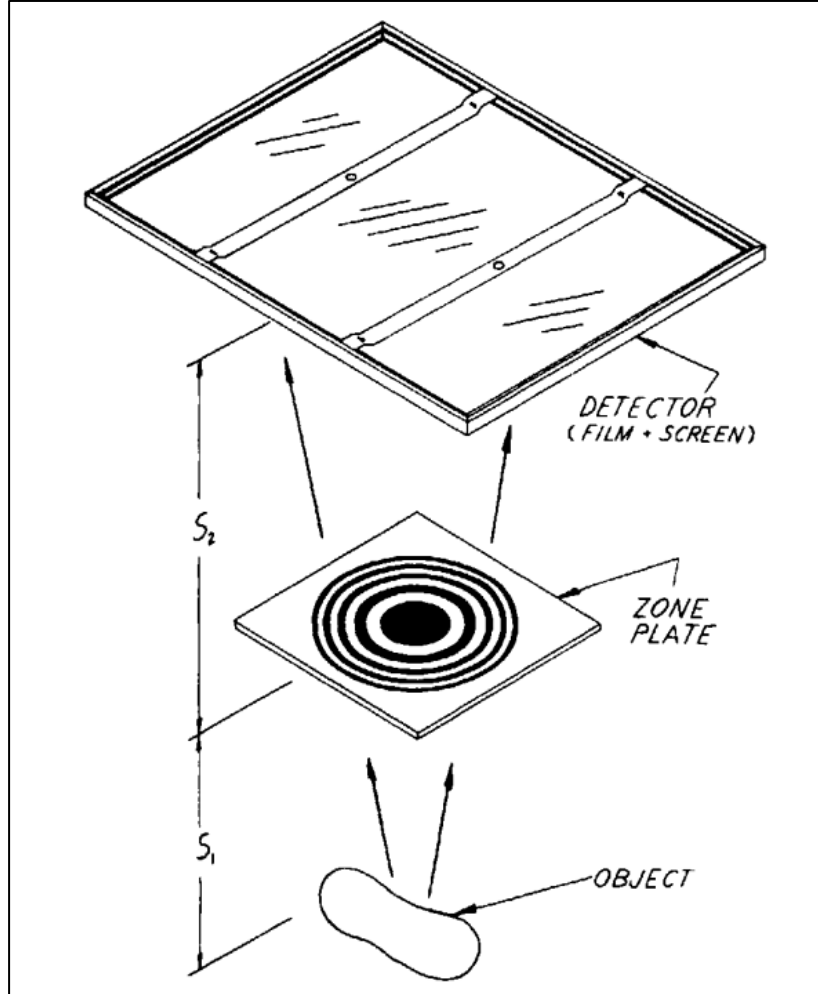
$$I_O = I_{PSF} \otimes \text{Random pinhole array}$$

$$I_R = I_O * I_{PSF}$$



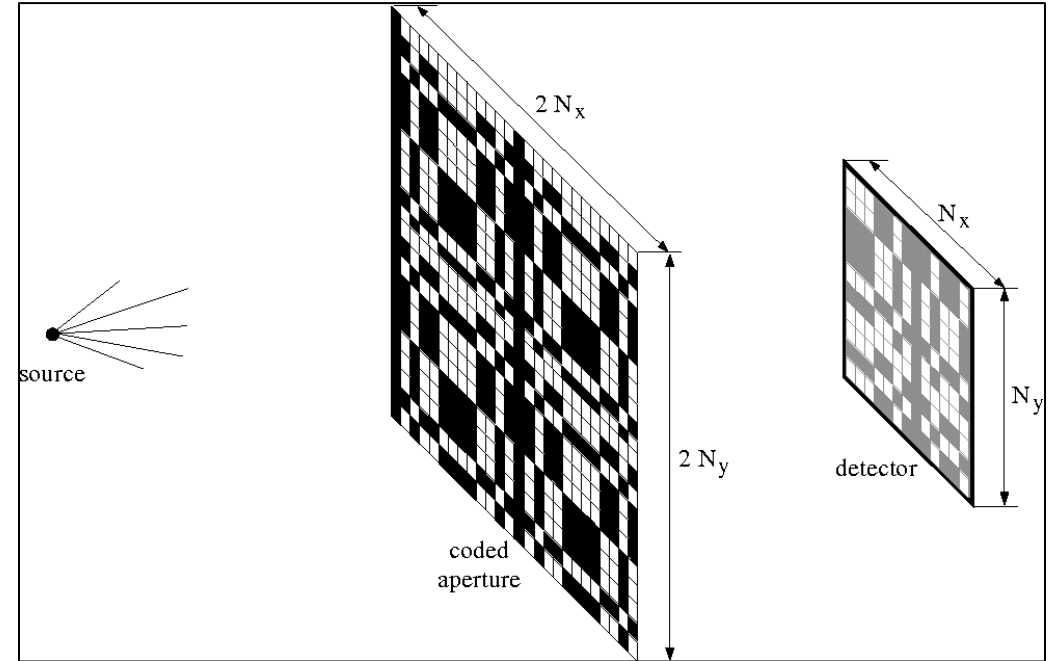
A. Vijayakumar and J. Rosen, *Photonics spectra Magazine* March 2020



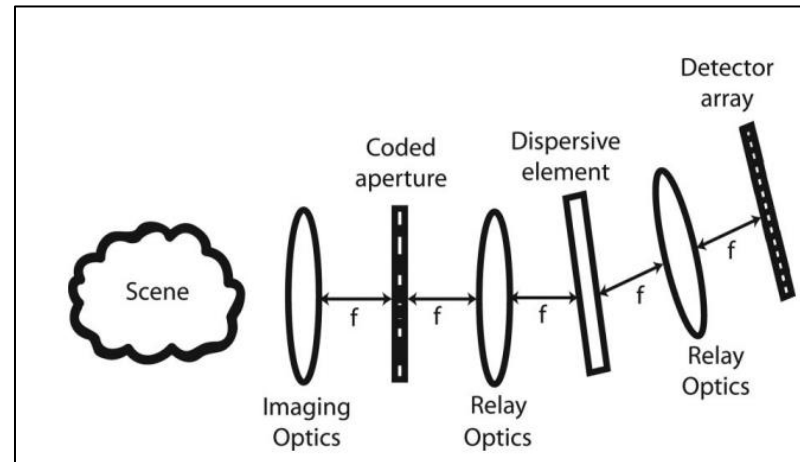


Tipton, et. al. *Radiology*, 112(1), 155–158.

# Coded aperture Imaging methods



Busboom, et. al. *Experimental Astronomy*, 8, 97–123 (1998)



Wagadarikar, et. al. *Appl. Opt.* 47, B44-B51 (2008)



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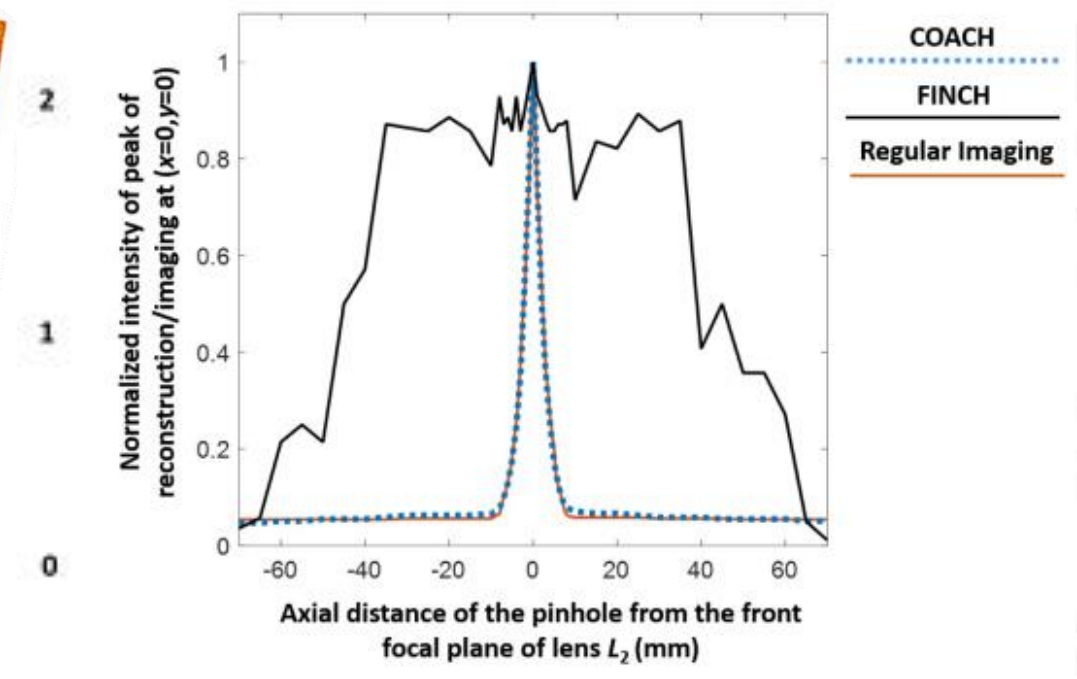
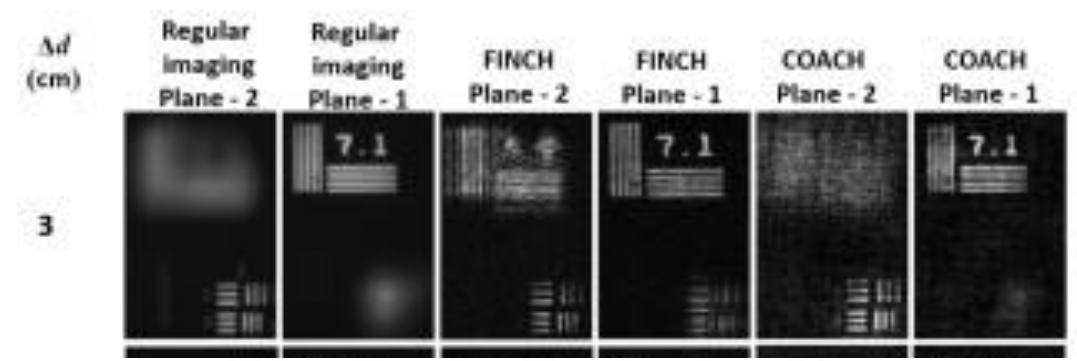
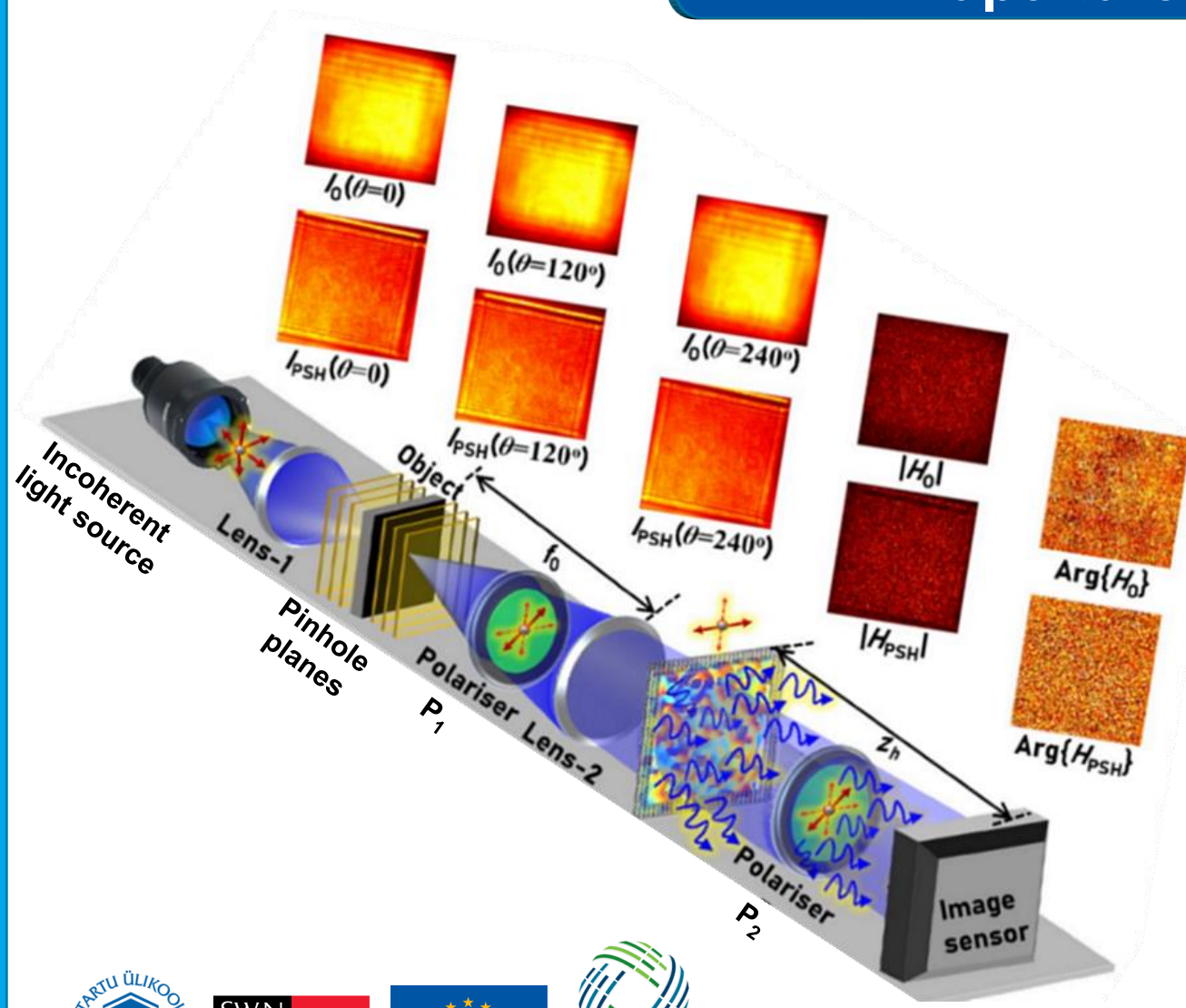
Aperture engineering

New capabilities and applications



# Incoherent digital holography meets coded aperture Imaging technology

Coded aperture correlation holography (COACH)





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# Outline

Incoherent digital holography

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Interferenceless coded aperture correlation holography

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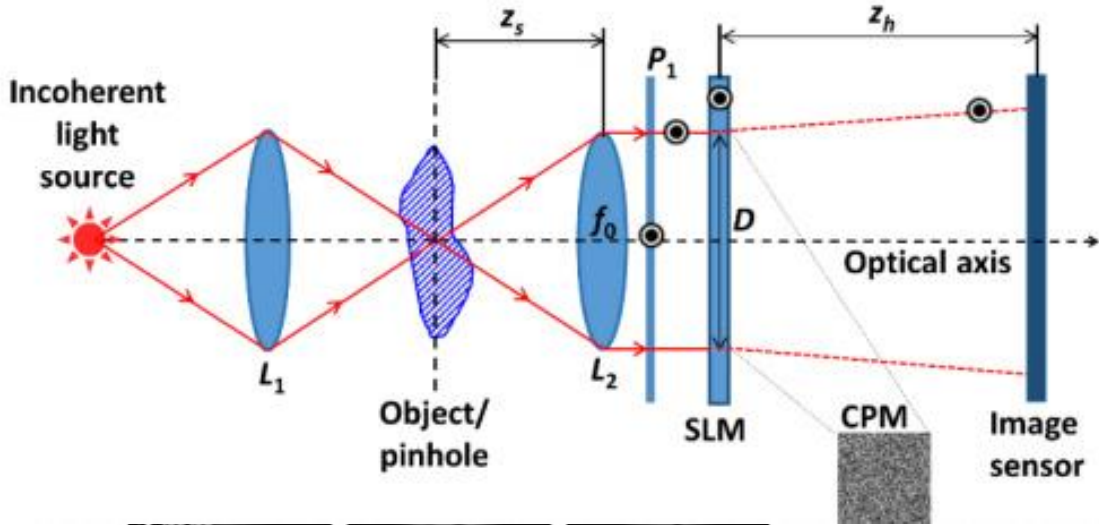
Aperture engineering

New capabilities and applications

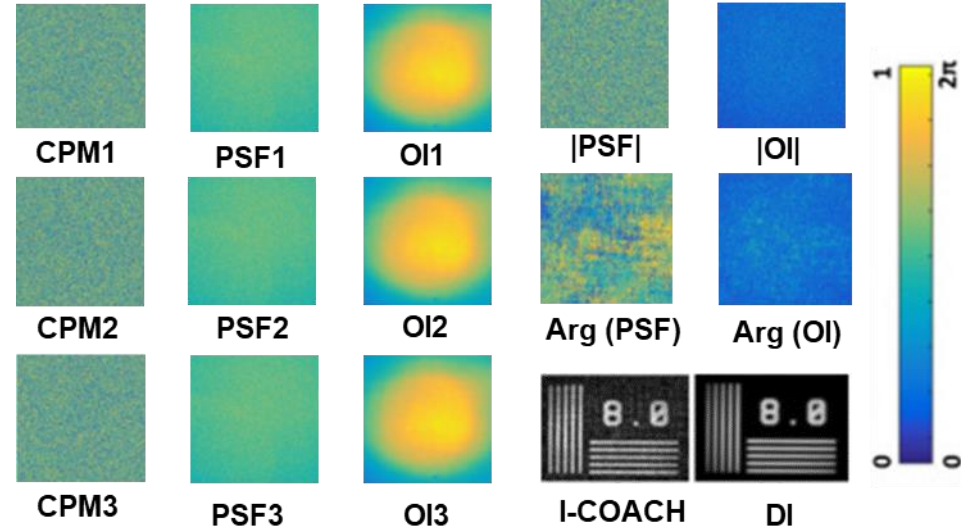


# Incoherent holography without two-beam interference

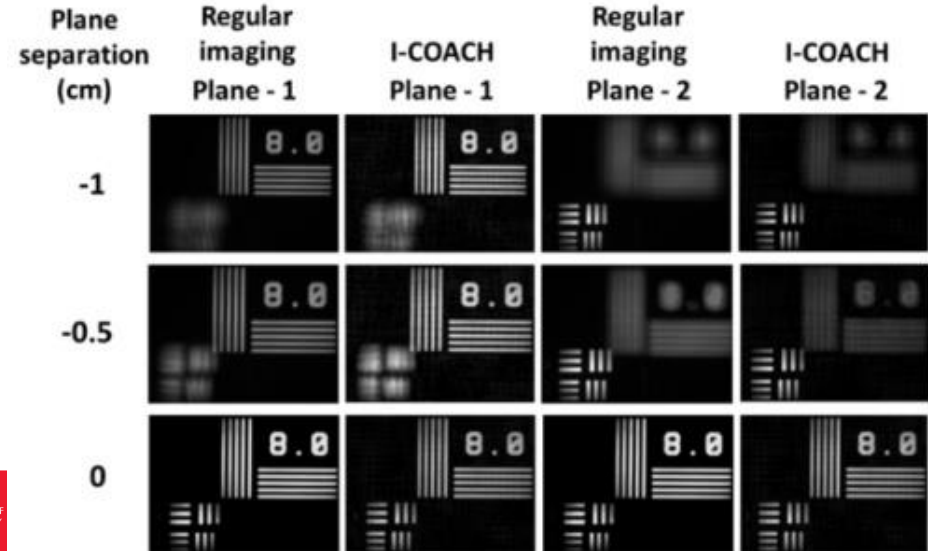
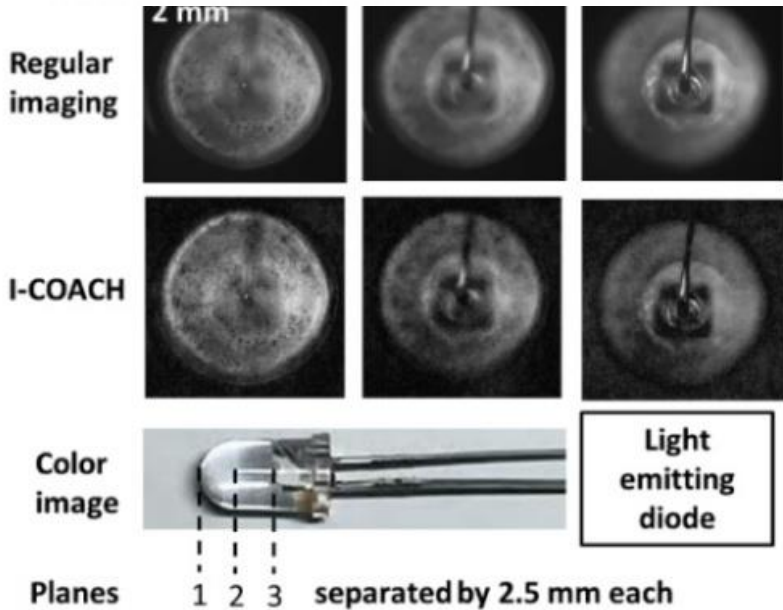
Interferenceless COACH (I-COACH)



2D imaging results



3D imaging results



3D imaging results



CIPHR





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Incoherent digital holography

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New capabilities and applications



# Non-Linear Reconstruction

Reconstruction methods

Lucy Richardson algorithm

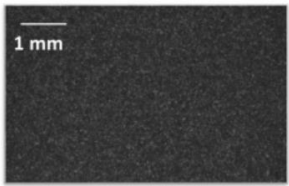
Phase-only filter

Matched filter

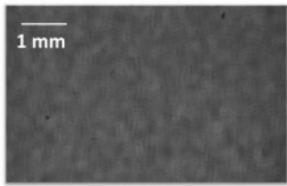
Regularized filter

Deep learning

Wiener filter



PSF



OI



$$I_{IMG} = I_{OBJ} * I_{PSF}$$

$$I_{IMG} = \mathcal{F}^{-1} \{ |\tilde{I}_{OBJ}|^0 \exp[i \cdot \arg(\tilde{I}_{OBJ})] |\tilde{I}_{PSH}|^r \exp[-i \cdot \arg(\tilde{I}_{PSH})] \}$$

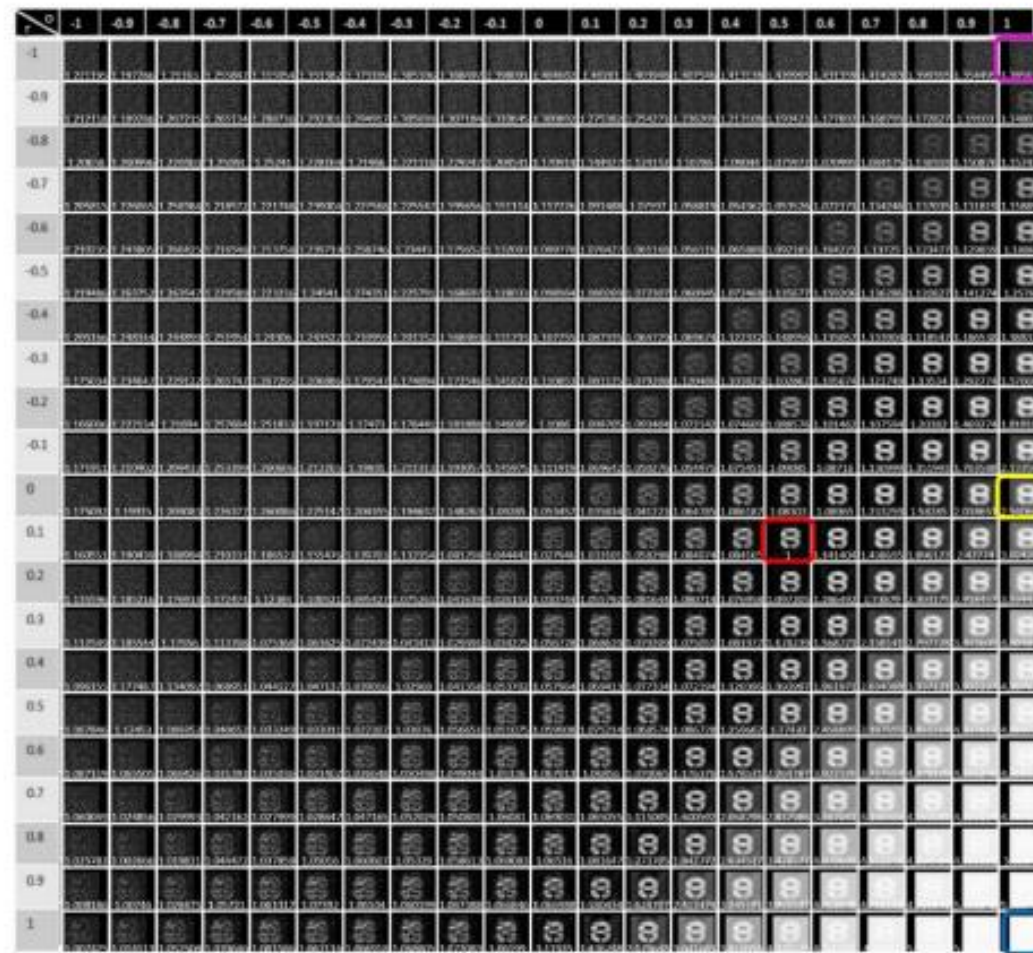


Figure of merit - Entropy

Matched filter

Inverse filter

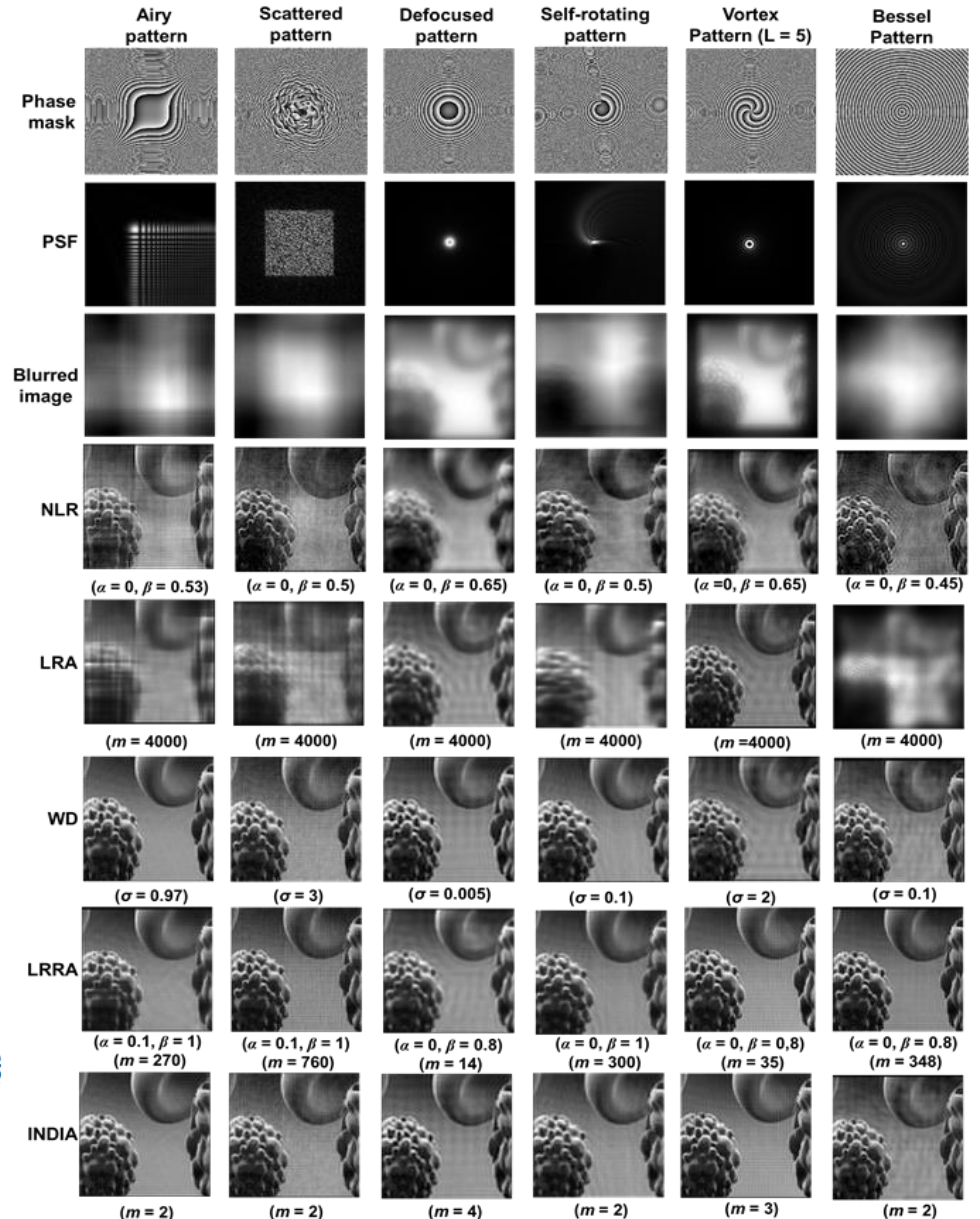
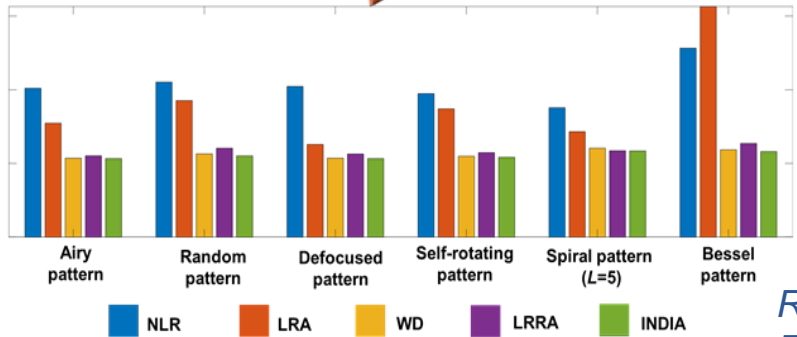
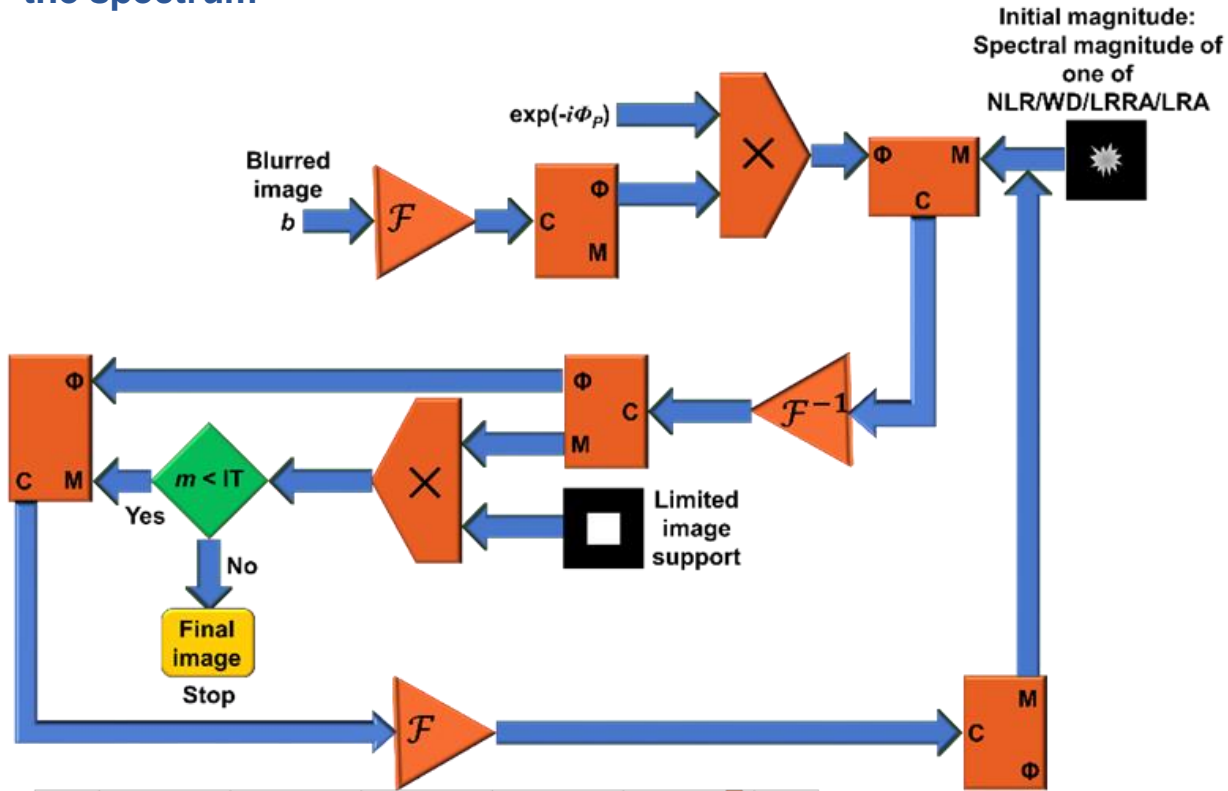
Phase-only filter

NLR





Majority of an object's information is present in the phase of the spectrum



Reconstruction methods





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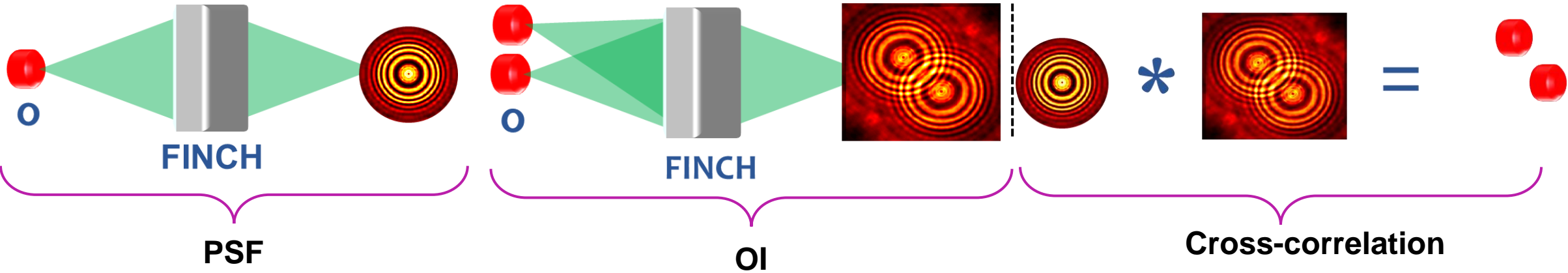
Aperture engineering

New capabilities and applications





# FINCH as a Coded Aperture Imaging System



Aperture Engineering + Advanced capabilities

Optical microscope images

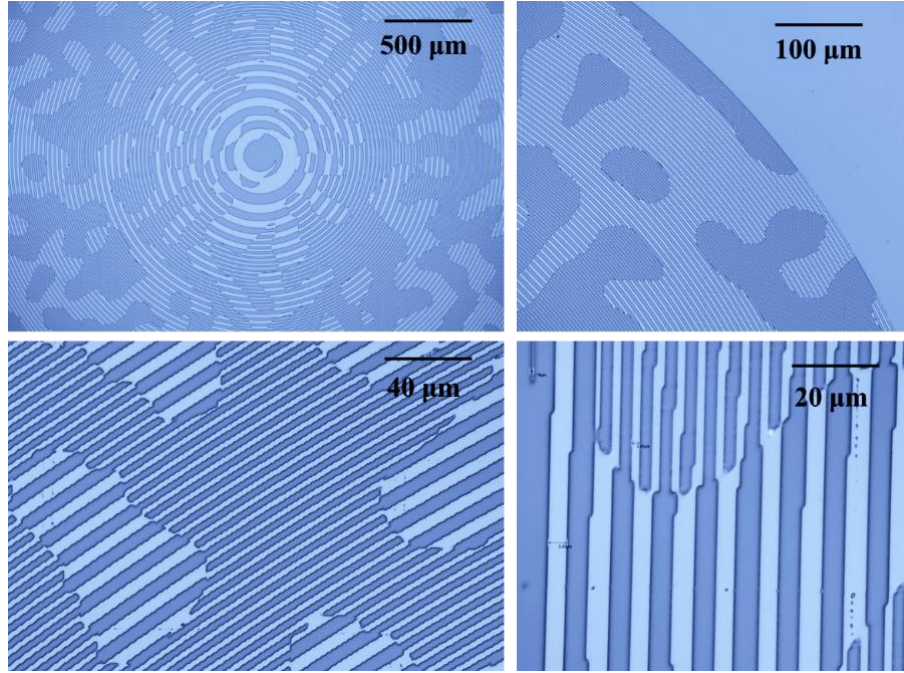
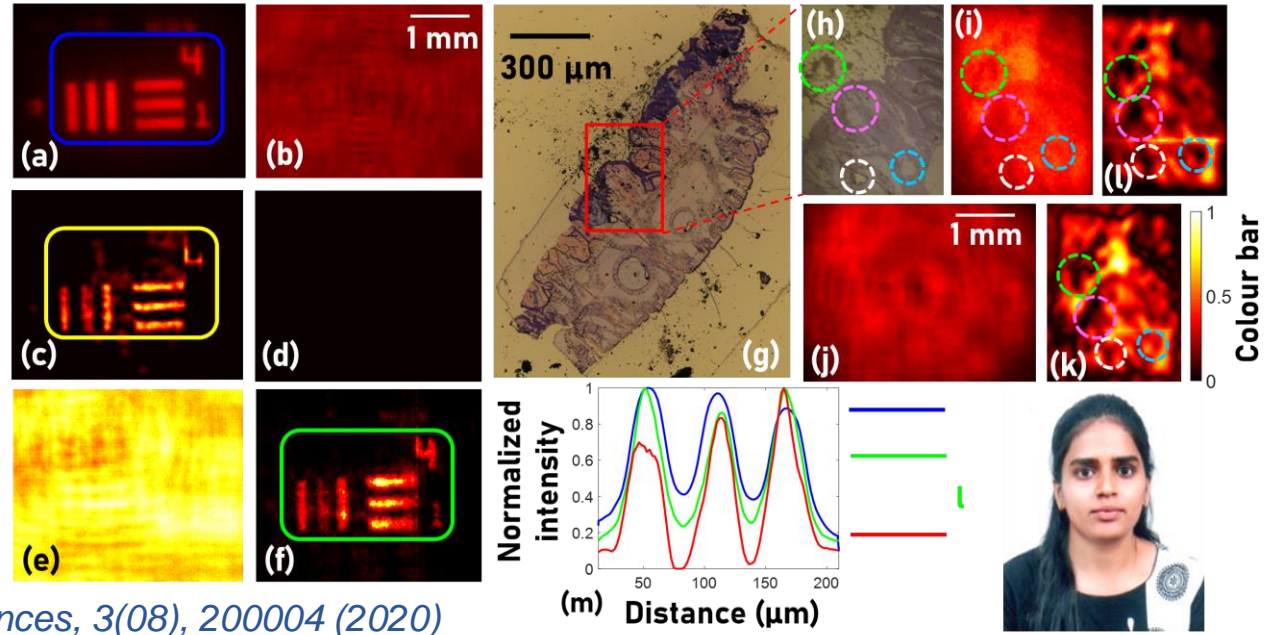


Image reconstruction



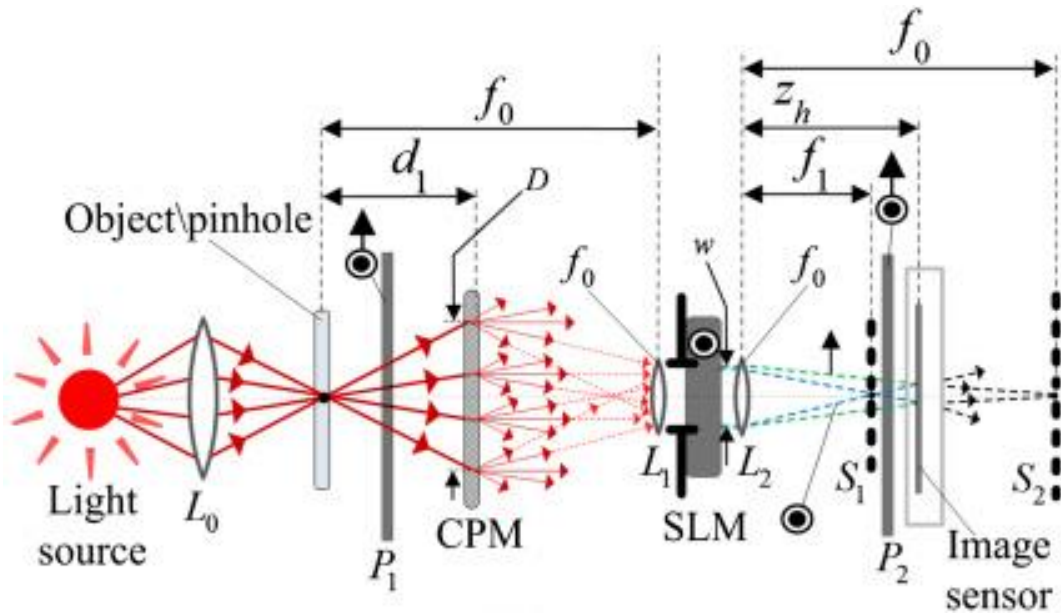
Ms. Francis GA (Doctoral student)

Anand, et. al. *Opto-Electronic Advances*, 3(08), 200004 (2020)  
 Arockiaraj, et. al. *J. Opt*, 26, 3 (2024)

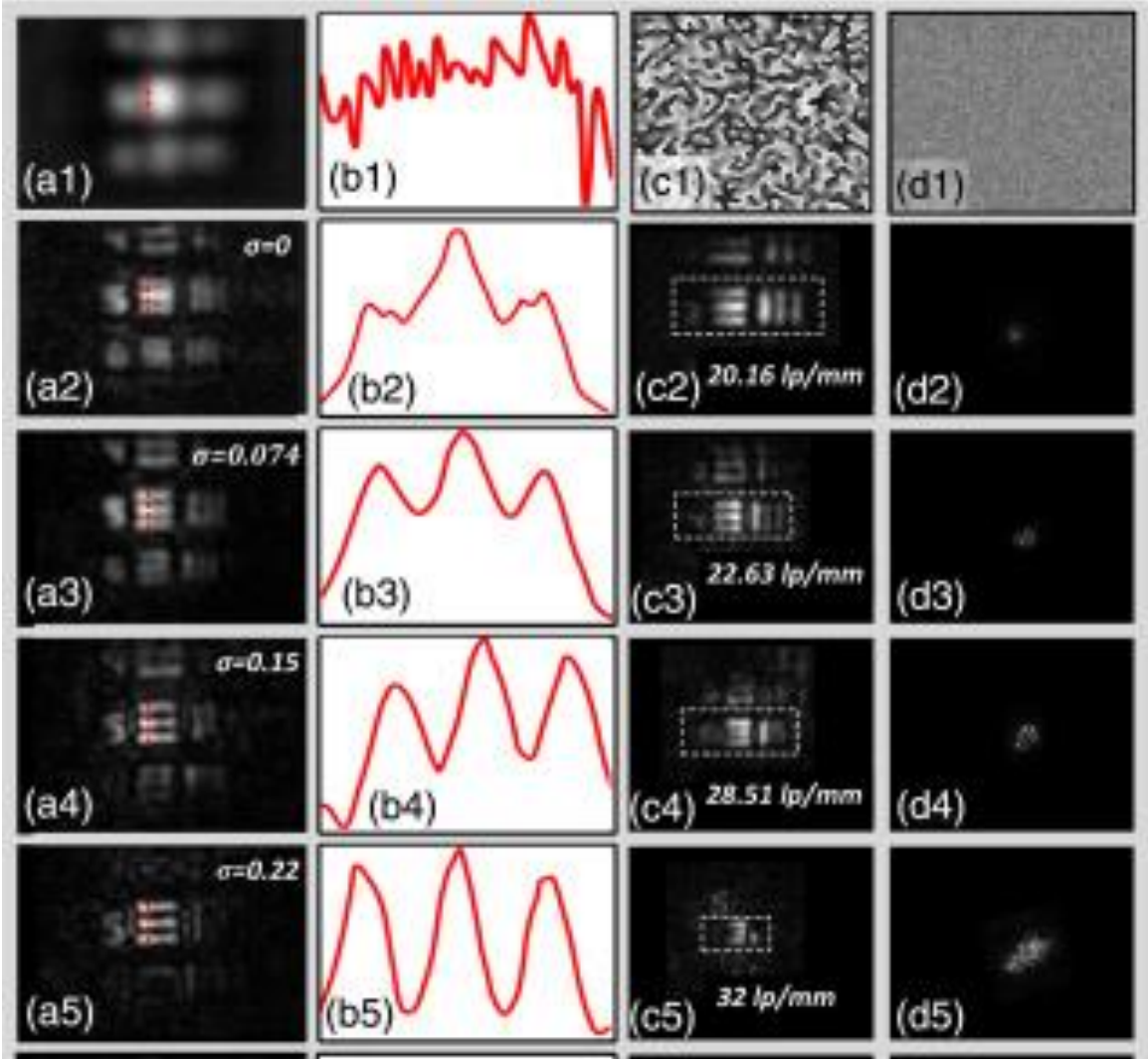


# FINCH-COACH Super Resolution System

Aperture Engineering + Advanced capabilities



Resolution enhancement of an order (10 times) was demonstrated

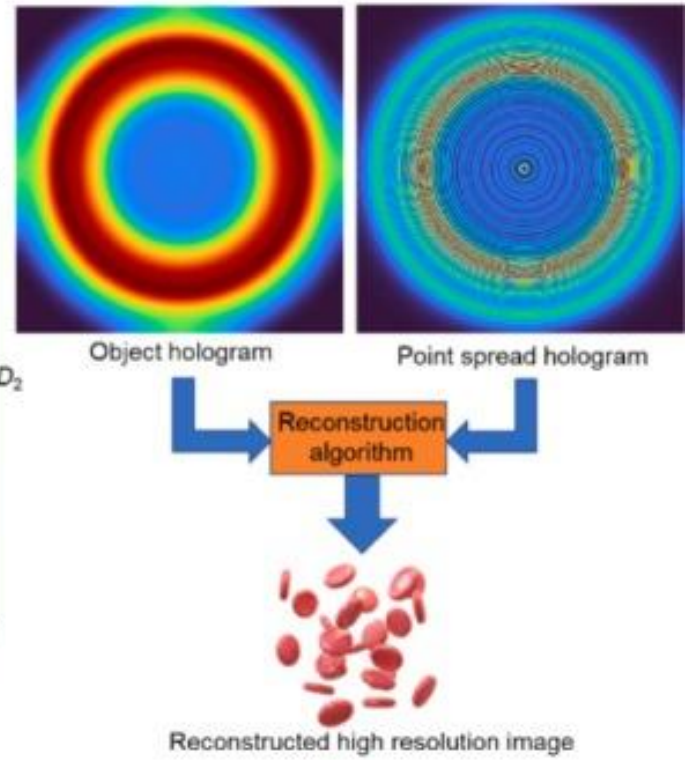
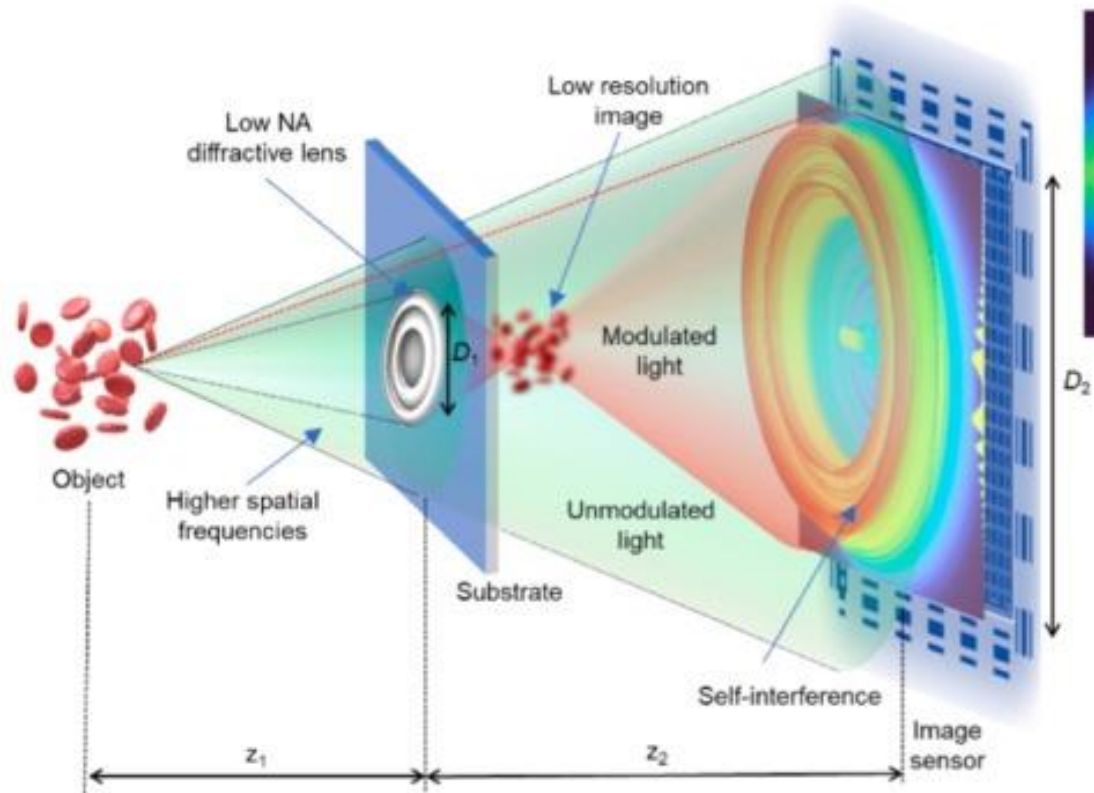


Y. Kashter, A. Vijayakumar, and J. Rosen, *Optica* 4, 932-939 (2017).



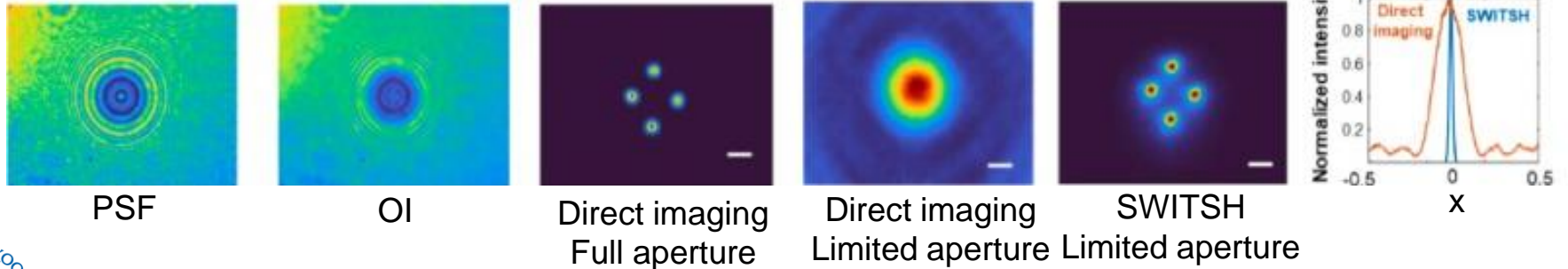
# Self Wavefront Transverse splitting Holography

Aperture Engineering + Advanced capabilities

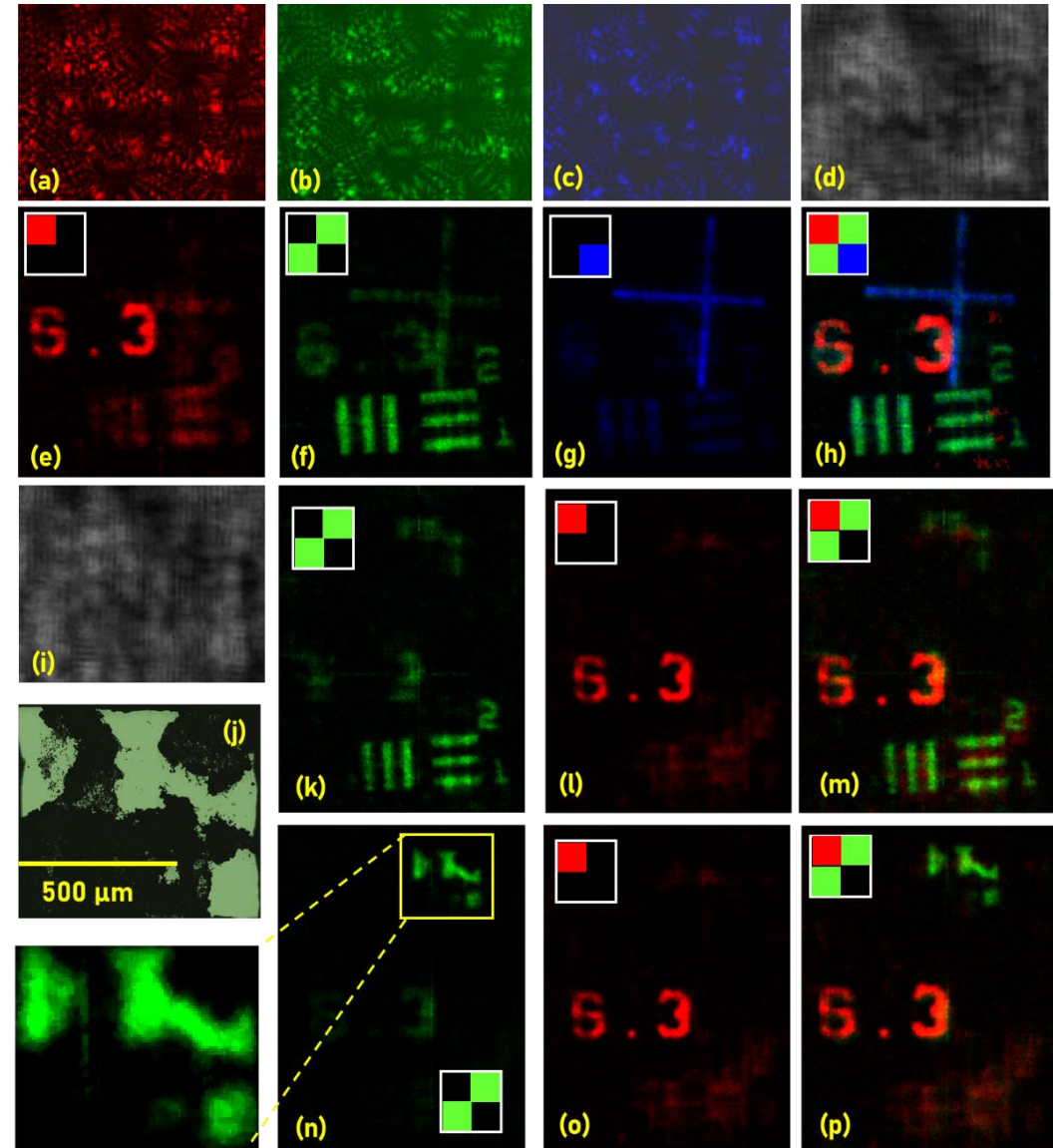
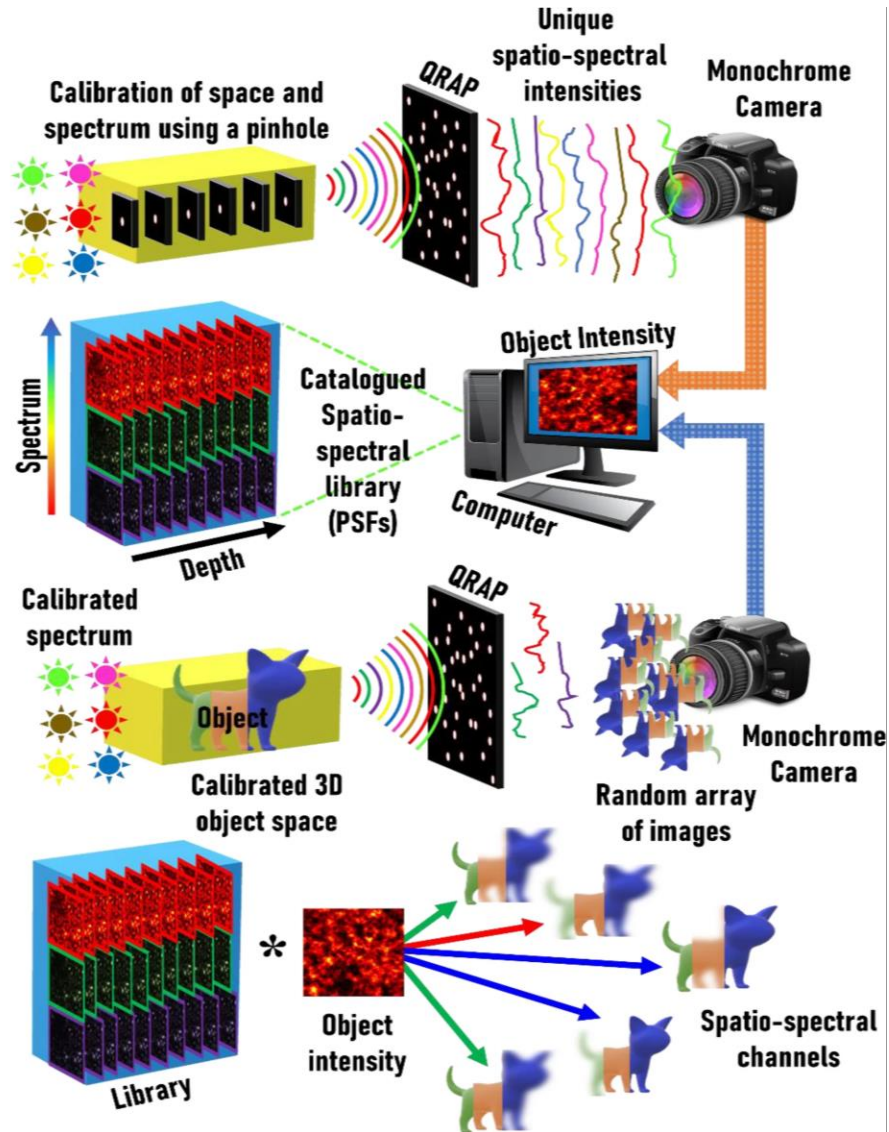


Ms. Narmada J  
(Doctoral student)

**Resolution enhancement of an order (10 times) was demonstrated**



# 5D Imaging system in 3D space, spectrum and time

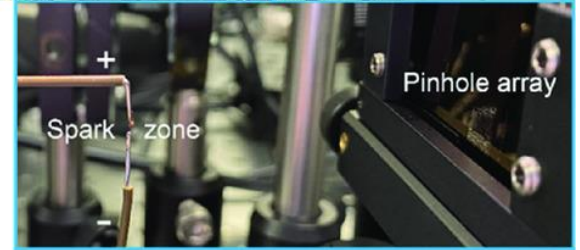
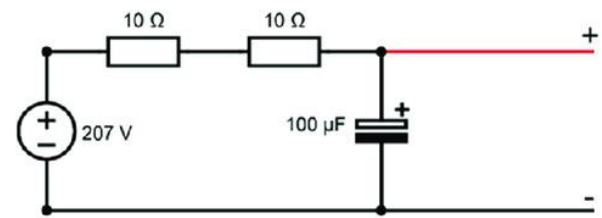
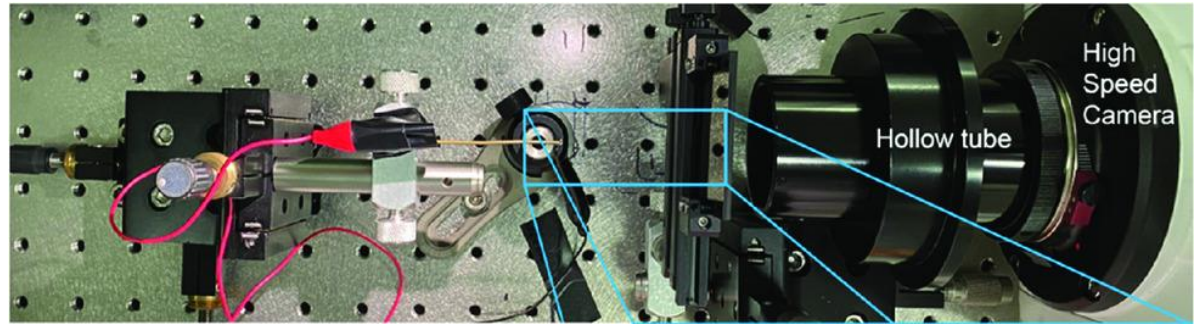
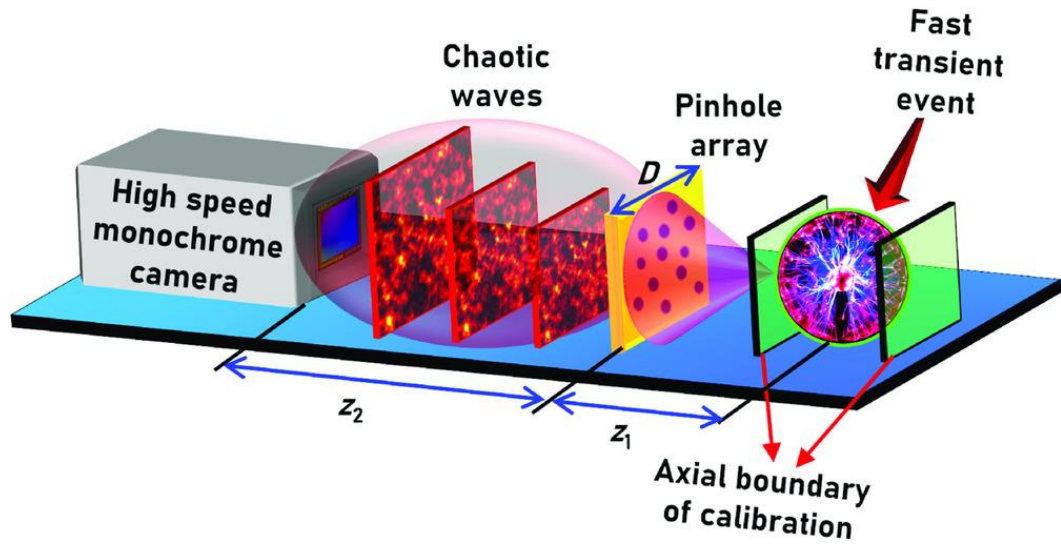


Anand, et. al. Sci. Rep. 3, 10, 1 (2020).

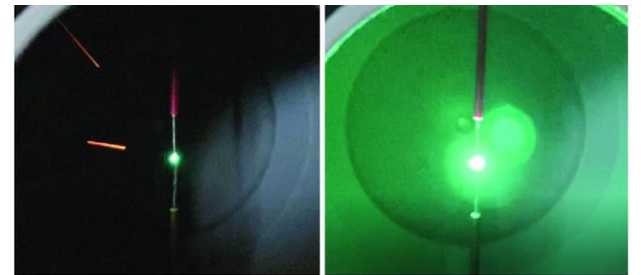
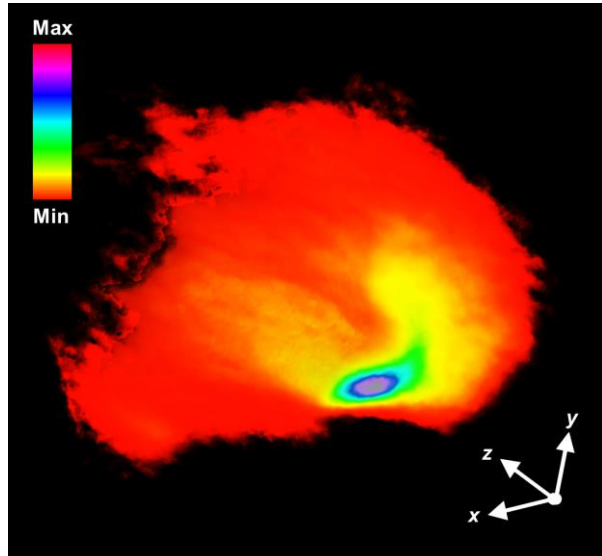
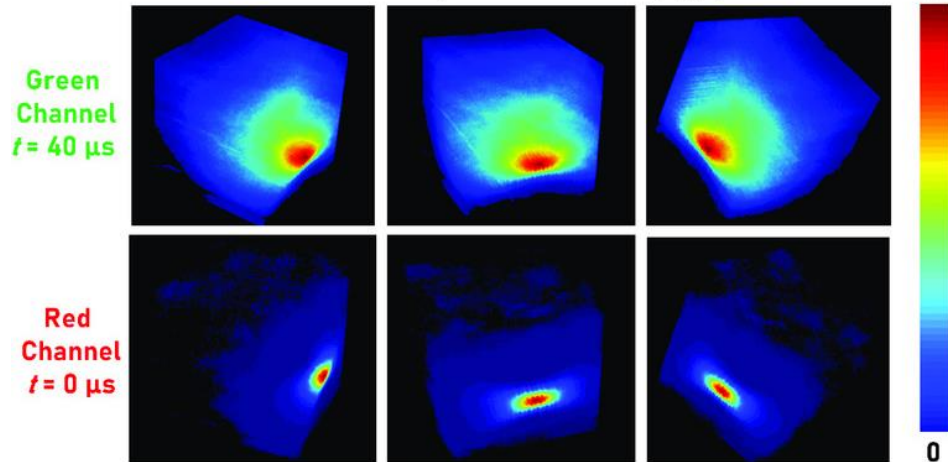


# Single Shot Tomography

Aperture Engineering + Advanced capabilities



Intensity cube data in 3D (x,y,z)

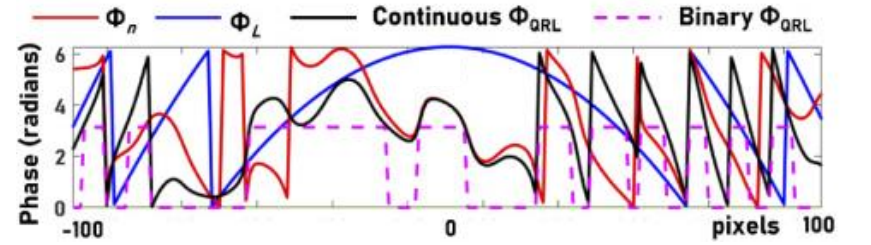
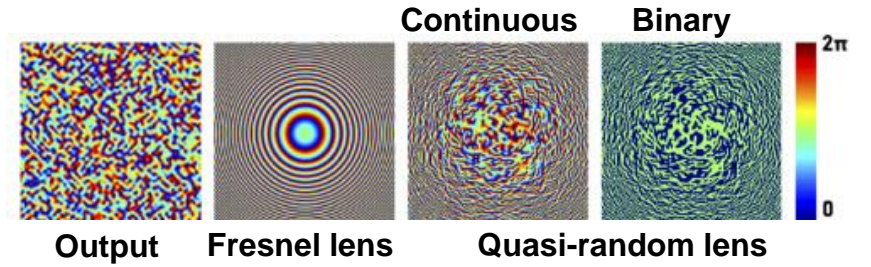
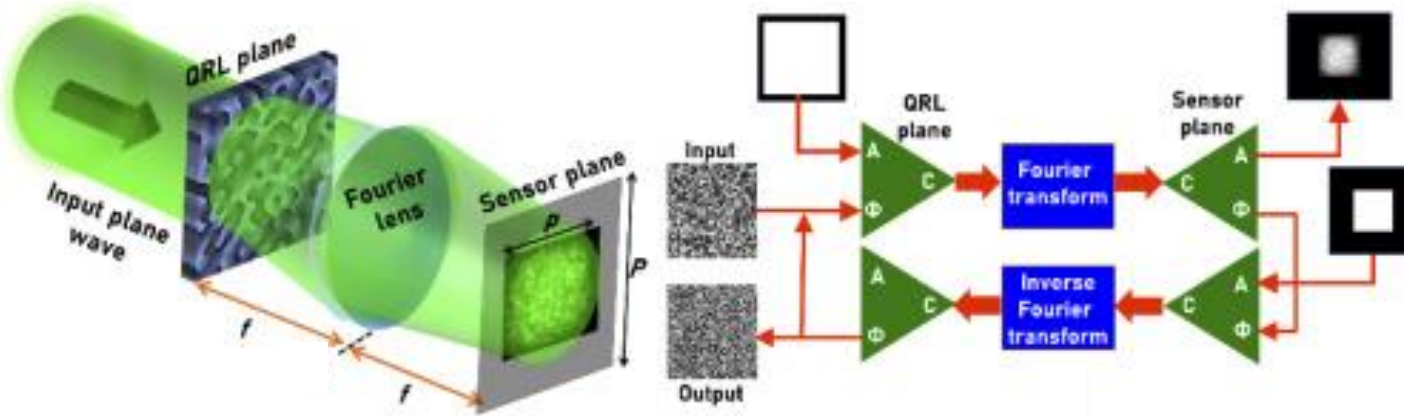




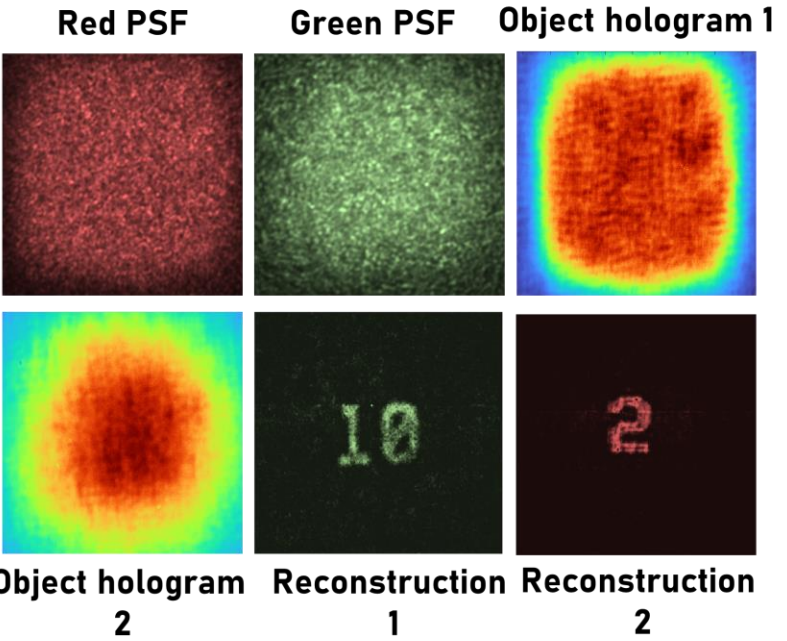
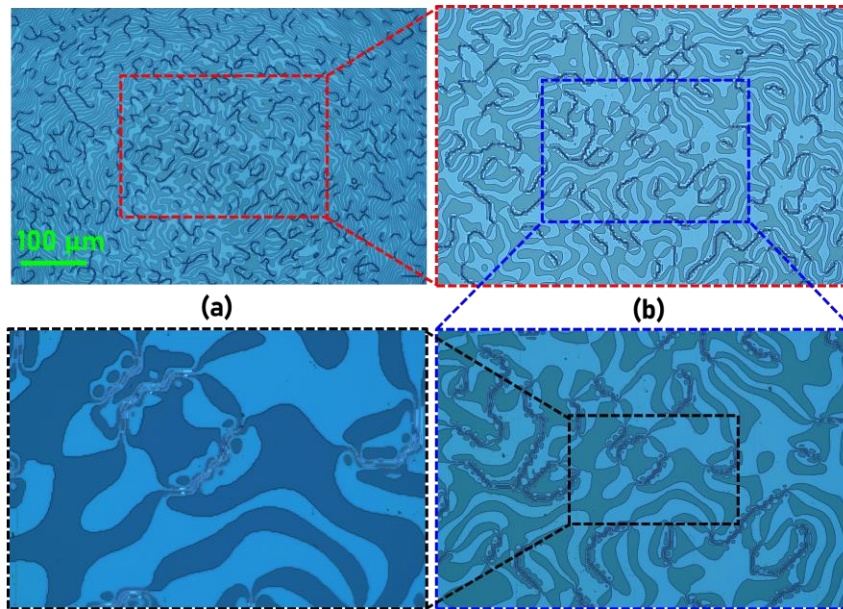


# 5D imaging with a quasi-random lens

Aperture Engineering + Advanced capabilities



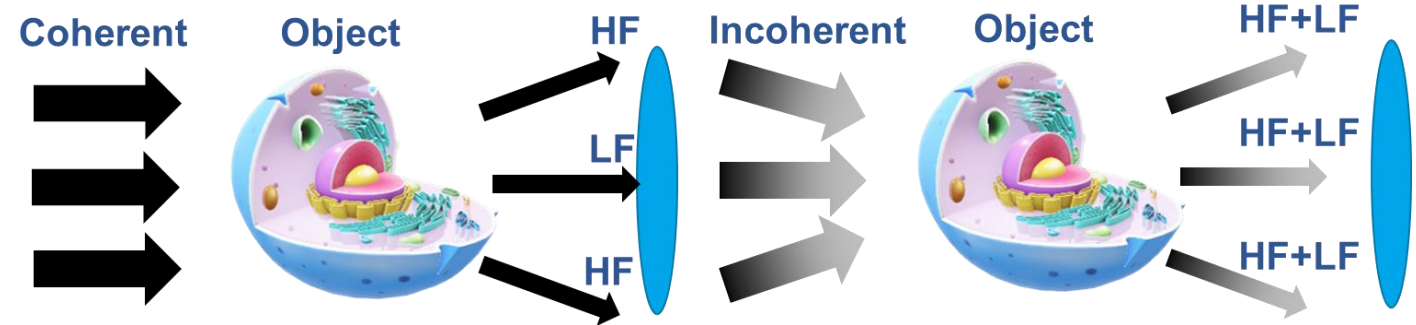
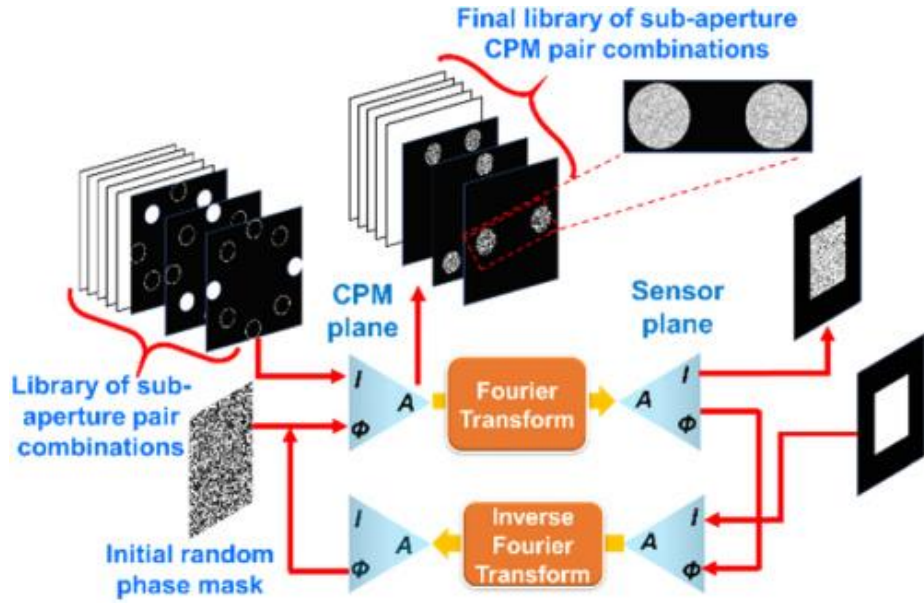
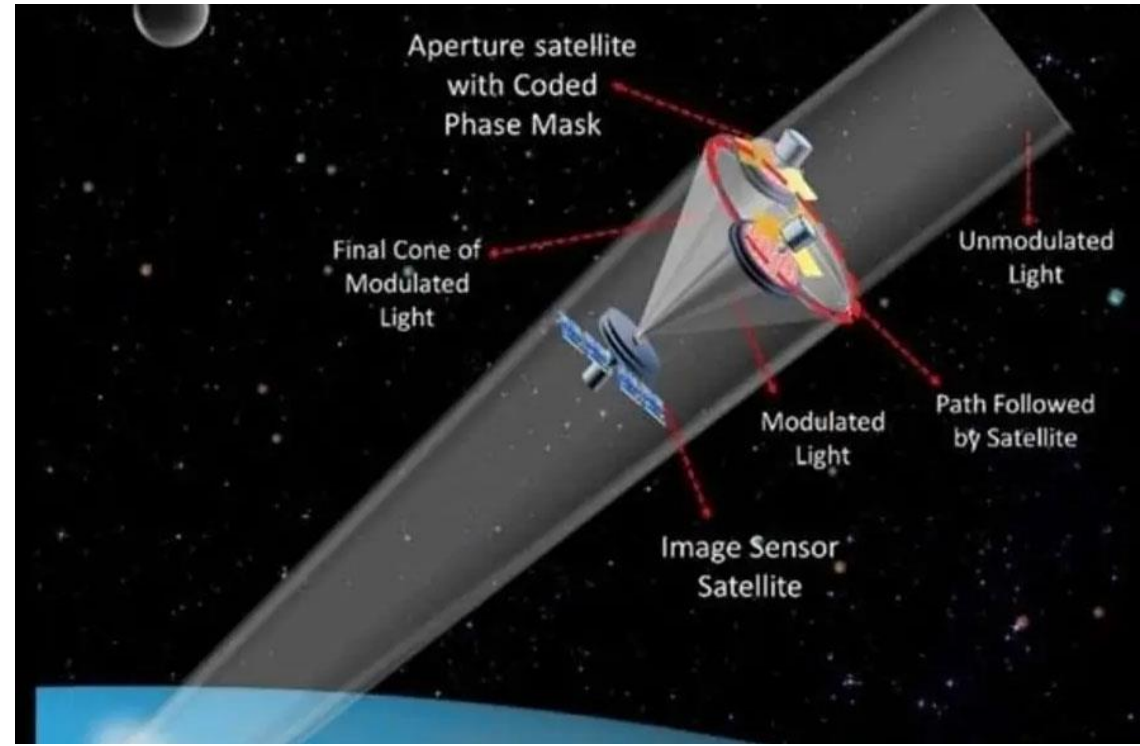
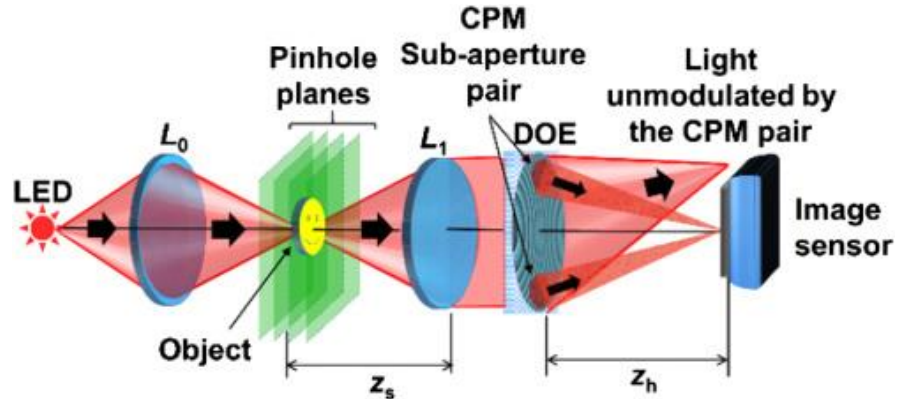
Optical microscope images





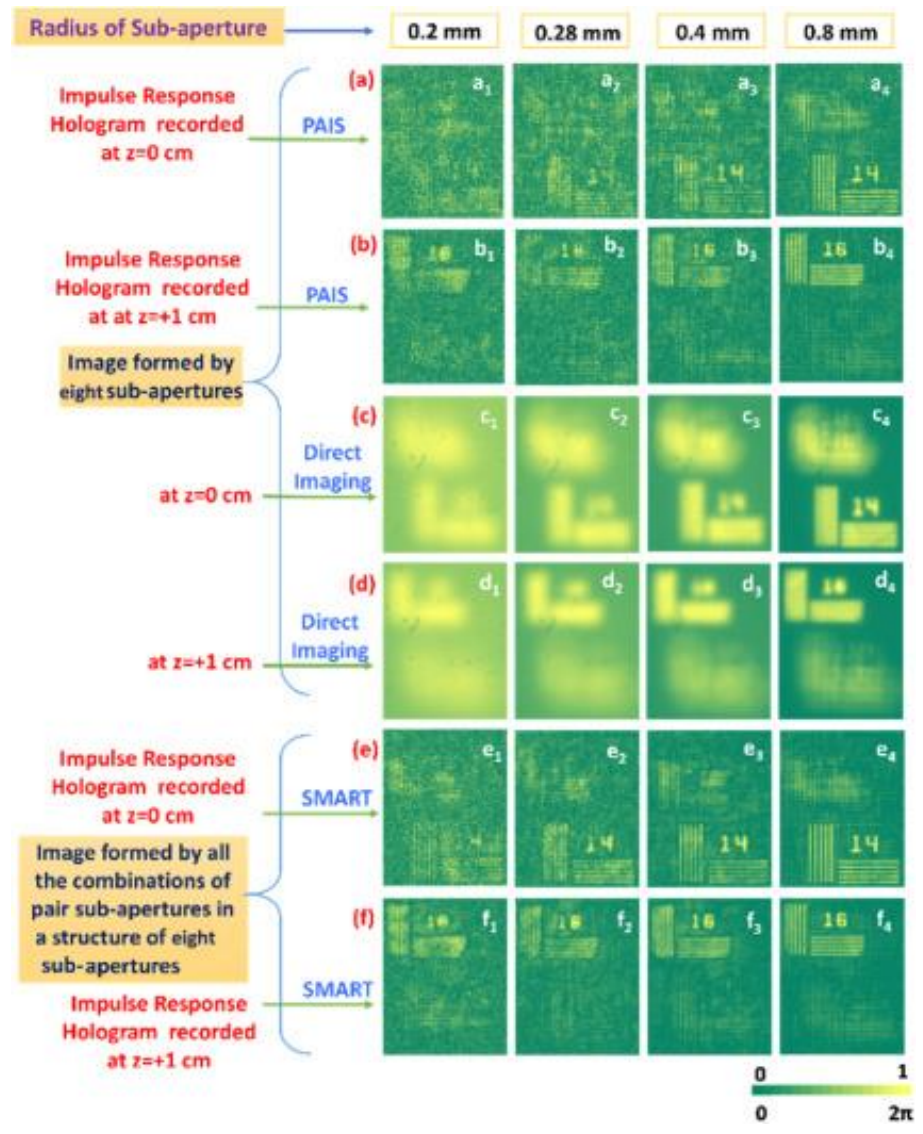
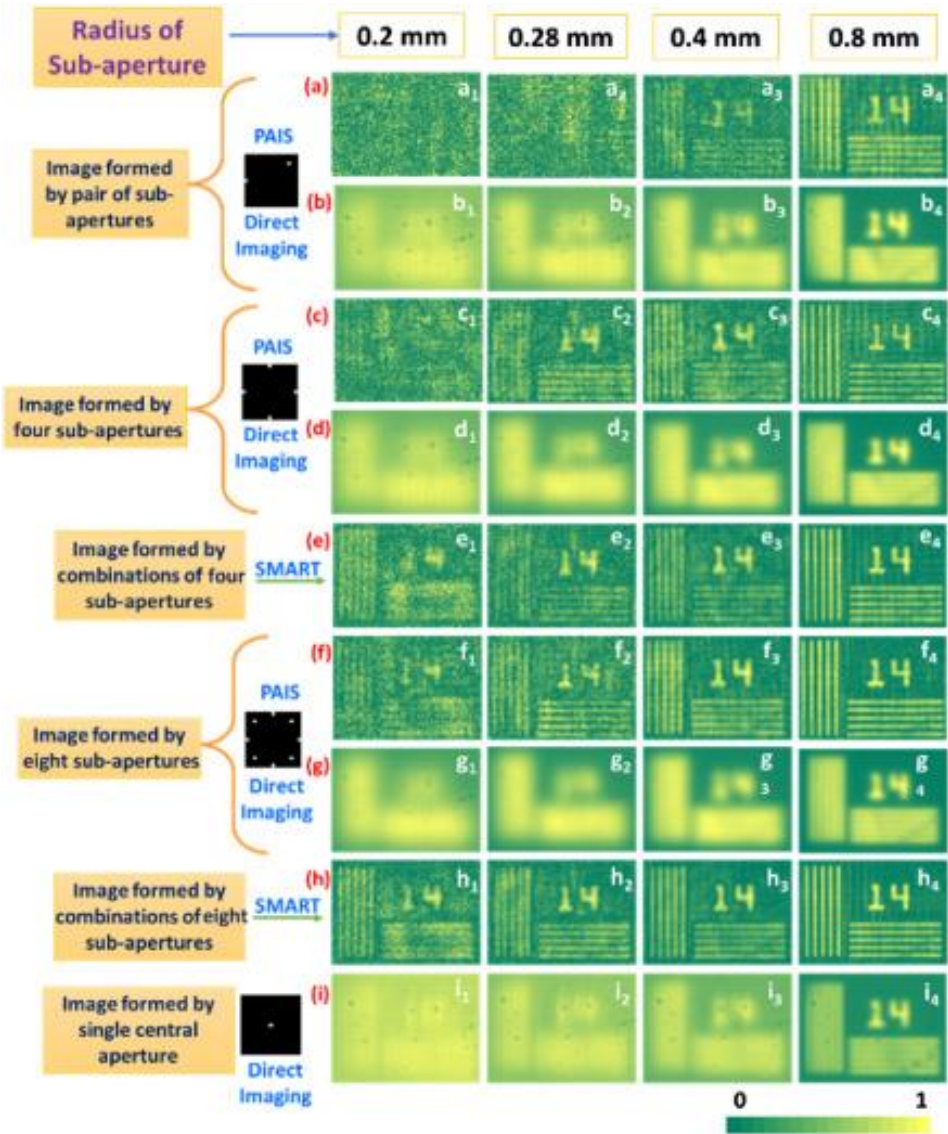
# Satellite Telescope with I-COACH

Aperture Engineering + Advanced capabilities



# Satellite Telescope with I-COACH

Aperture Engineering + Advanced capabilities

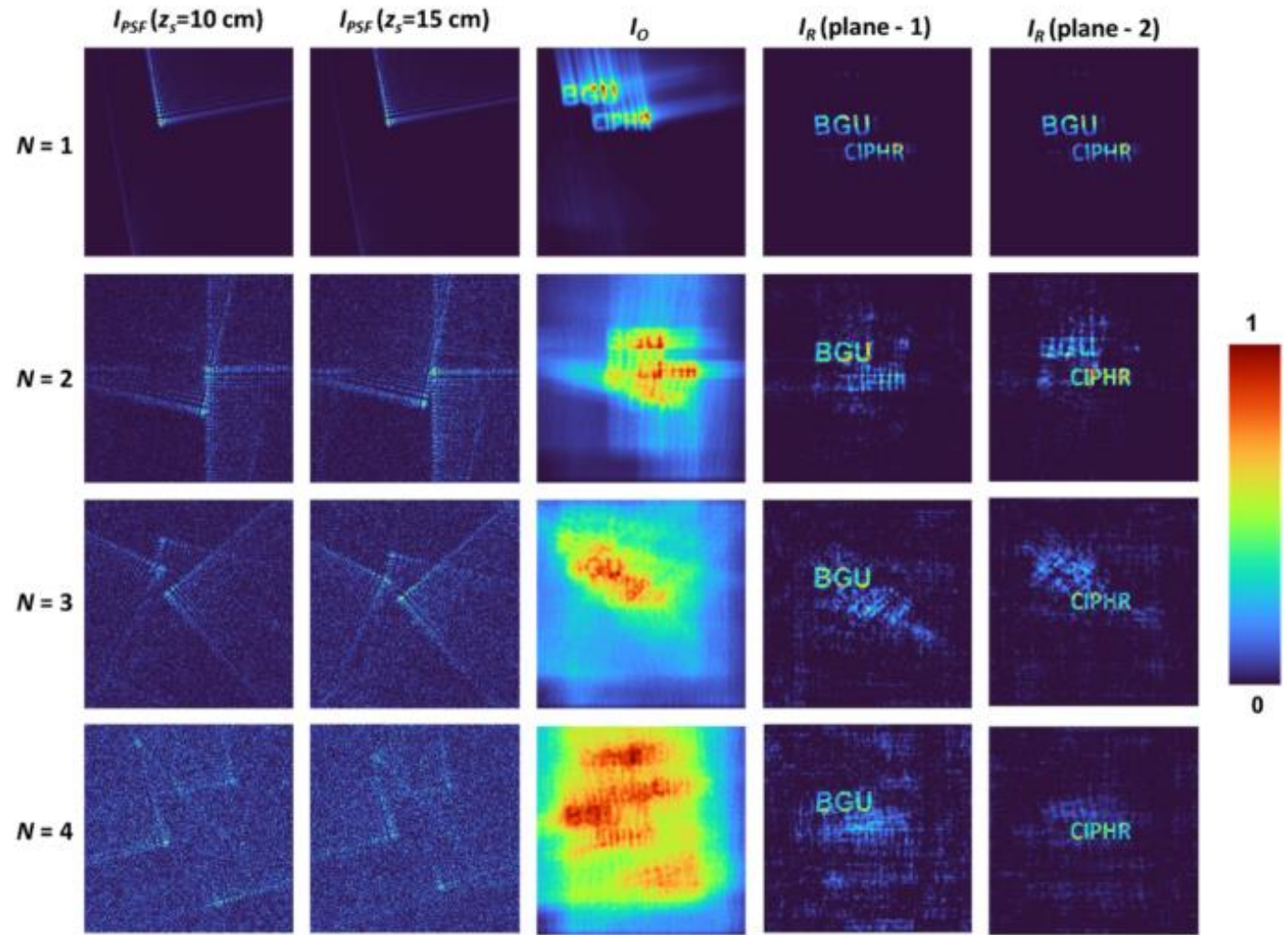
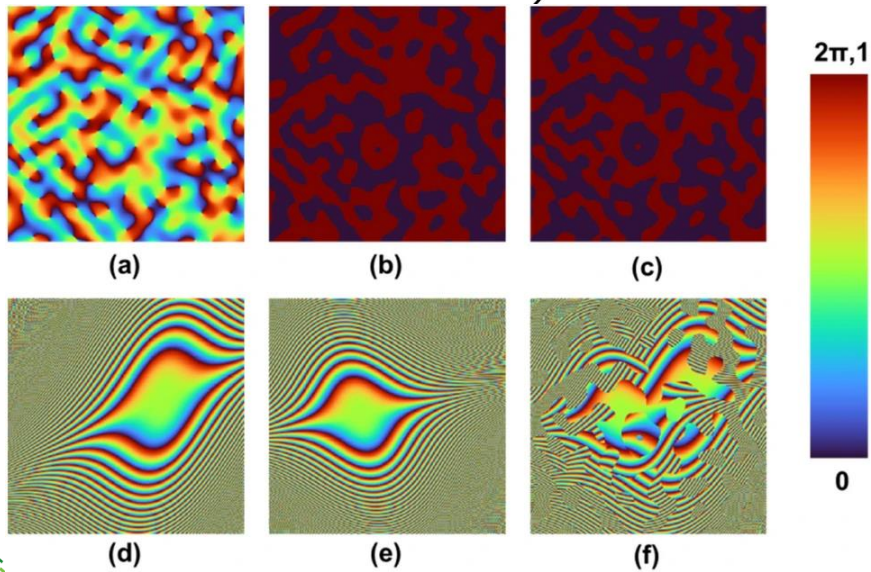
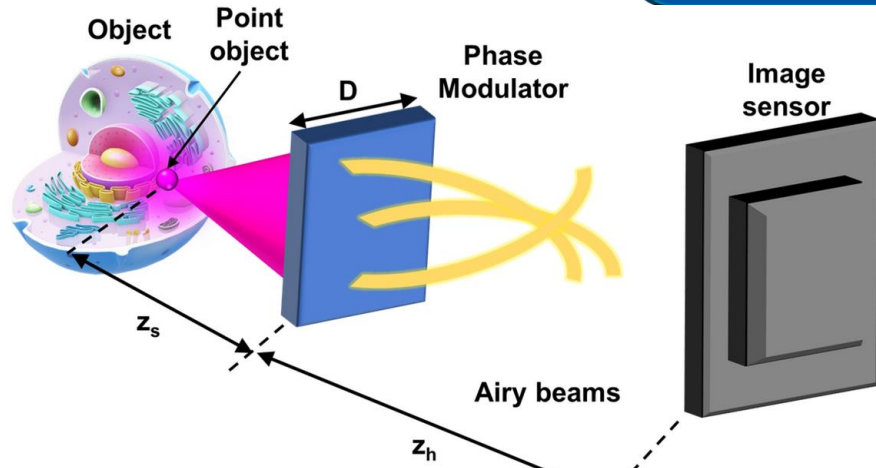


A. Bulbul, A. Vijayakumar, and J. Rosen, *Optica* 5, 1607-1616 (2018)  
 J. Rosen, A. Vijayakumar and A. Bulbul, US patent 11,445,125 (2022, Granted)



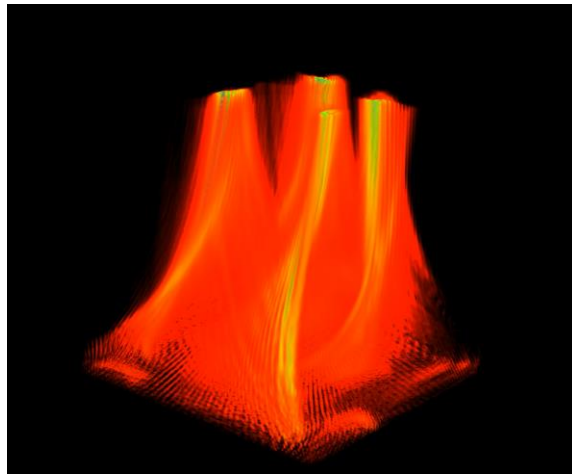
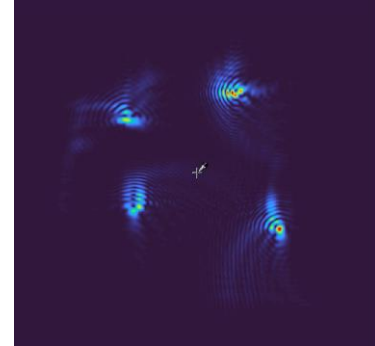
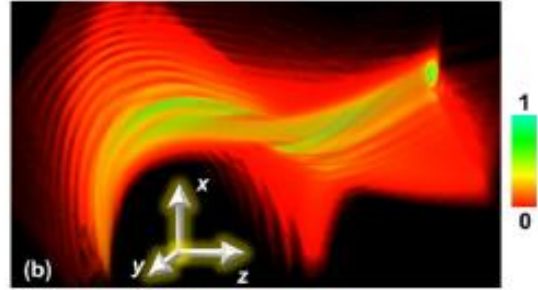
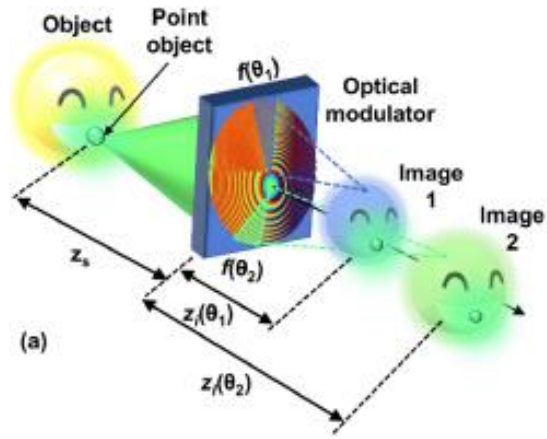
# Tuning axial resolution independent of lateral resolution – Airy beams ensemble

Aperture Engineering + Advanced capabilities

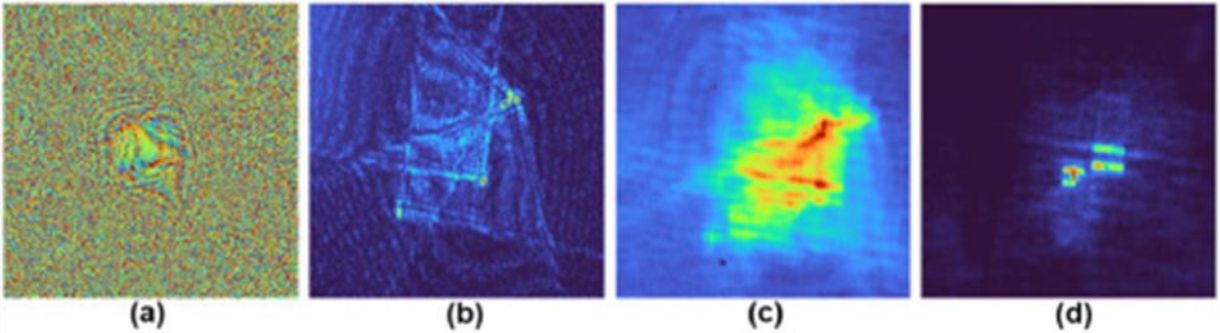


# Tuning axial resolution independent of lateral resolution – Self-rotating beams ensemble

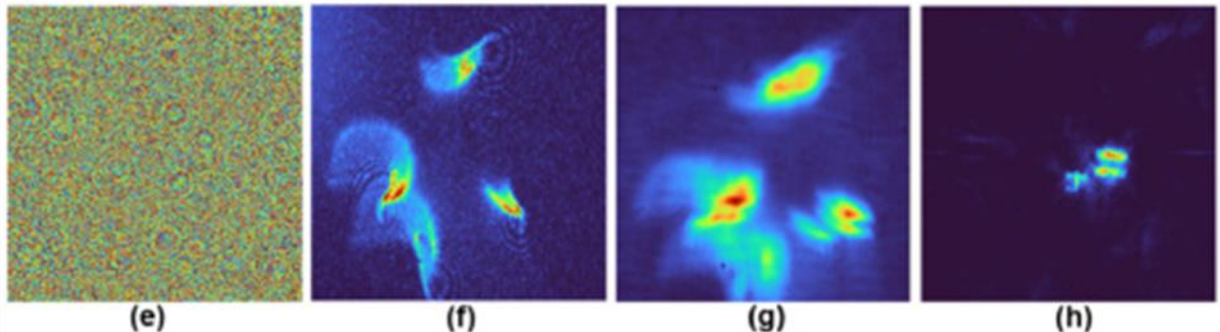
Aperture Engineering + Advanced capabilities



Airy beams



Self-rotating beams



Bleahu, et. al. *Opt. Express* 31, 26120-26134 (2023)

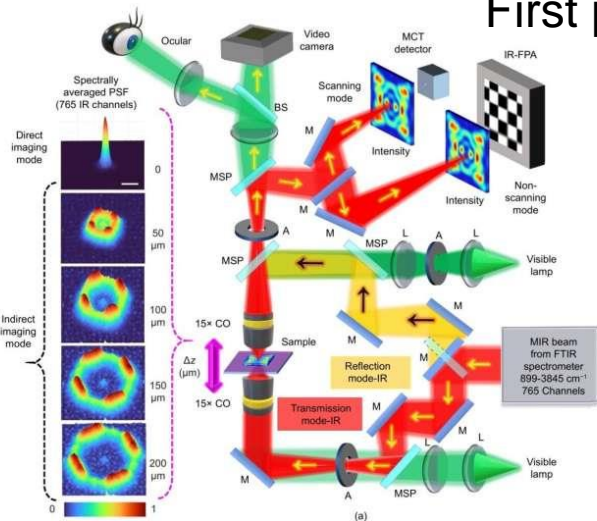
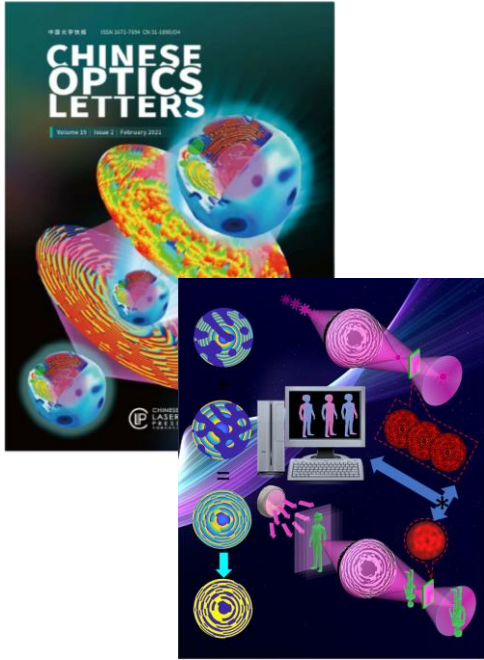


# News on Coded Aperture Imaging

作者简介



FINCH as CAI – Cover page of Chinese Optics Letters and Opto-Electronic Advances cash prize and outstanding research award (2021), First prize from RAITH systems



Lucy-Richardson-Rosen algorithm in Phys. Org, Spectroscopy news and Hot paper in 2022.

**Incoherent Hybrid Imaging System (INCHIS) – A Holographic hybridization technique for digital time travelling**

The diagram shows the experimental setup for INCHIS, including a point object, object distance, lens, axicon, and two cameras (Camera 1 and Camera 2). The process involves computational reconstruction to produce hybrid intensity patterns. The results are compared for Low depth of field, Hybrid, and High depth of field.

**PHYS ORG**

**IEEE Spectrum**

Depth of field tuning after recording pictures and videos – IEEE spectrum news and Phys. Org - 2023



Satellite telescope – Phys. Org, India Times and Economic Times in 2019



# Collaboration network

## Holography and structured light



Joseph Rosen  
(BGU)



Boaz Jessie  
Jackin (KIT)



Pierre  
Magistretti  
(KAUST)



Ravi Kumar  
(SRM-AP)



Andrew Forbes  
(WITS  
University)



Naresh Reddy  
(Latvia University)



Hasan Yilmaz  
(Bilkent  
University)



Etienne  
Brasselet  
(Bordeaux  
University)



Manoj Kumar  
(Kobe  
University)

## Advanced Manufacturing and Nanophotonics



Saulius Juodkazis  
(Swinburne)



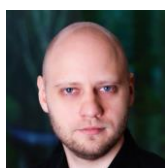
Aile Tamm  
(Tartu  
University)



Kaupo Kukli  
(Tartu  
University)



Mangirdas  
Malinauskas  
(Vilnius  
University)



Darius  
Gailevicius  
(Vilnius  
University)



Elena Ivanova  
(RMIT  
University)



Scott Singh  
(Scott Laser  
Piles and Fistula  
Center)



Milling Tania  
(Rajas College)



Andres  
Salumets  
(Tartu Univ)



Zoltan Vilagosh  
(Baroondara  
Health Center)

## Deep Learning



Rajesh Sharma,  
Tartu University

## Synchrotron imaging



Jitraporn Vongsvivut,  
Australian synchrotron





# Joint Activities

- Summer School 2024/2025
- International Conference 2025
- Dual Doctoral degree
- International Master degree
- Joint Research
- Joint Grant Consortium Applications – ERC
- Joint Estonian Grant Applications

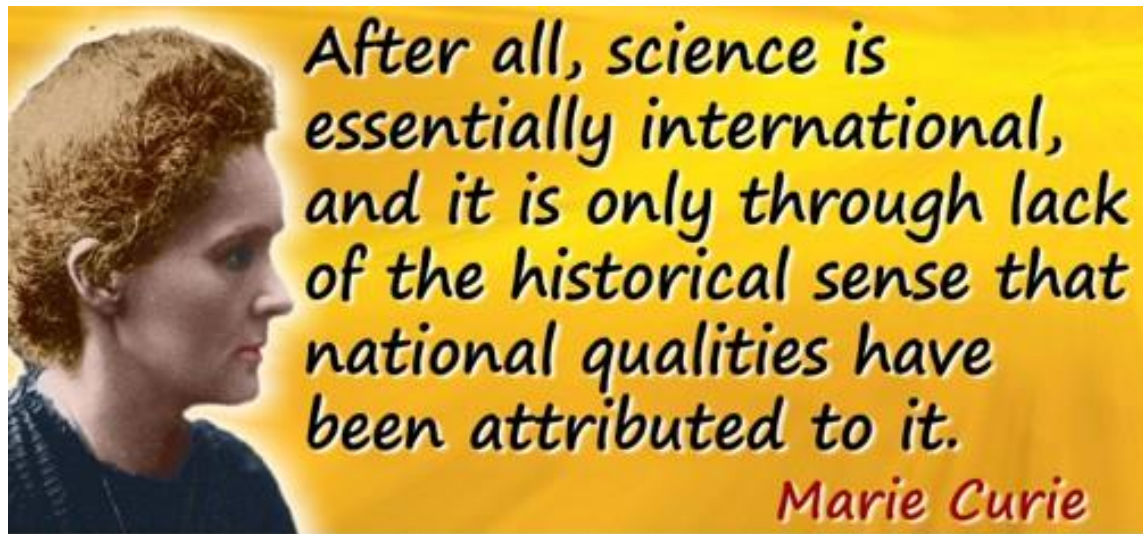




UNIVERSITY OF TAFE







unitartu



tartuuniversity

**Funded projects  
(PhD and Postdoc  
positions)**

